**RESEARCH PAPER** 



# SALTUS probe class space mission: observatory architecture and mission design

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ABSTRACT. We describe the space observatory architecture and mission design of the Single Aperture Large Telescope for Universe Studies (SALTUS) mission, a National Aeronautics and Space Administration (NASA) Astrophysics Probe Explorer concept. SALTUS will address key far-infrared science using a 14-m diameter <45 K primary reflector (M1) and will provide unprecedented levels of spectral sensitivity for planet, solar system, and galactic evolution studies and cosmic origins. Drawing from Northrop Grumman's extensive NASA mission heritage, the observatory flight system is based on the LEOStar-3 spacecraft platform to carry the SALTUS Payload. The Payload is comprised of the inflation control system, sunshield module (SM), cold corrector module (CCM), warm instrument electronics module, and primary reflector module (PRM). The 14-m M1 is an off-axis inflatable membrane radiatively cooled by a two-layer sunshield (~1000 m<sup>2</sup> per layer). The CCM corrects for residual aberration from M1 and delivers a focused beam to two instruments-the High-Resolution Receiver (HiRX) and SAFARI-Lite. The CCM and PRM reside atop a truss-based composite deck that also provides a platform for the attitude control system. The SALTUS 5-year mission lifetime is driven by a two-consumable architecture: the propellant system and the inflation control system. The core interface module (CIM), a multi-faceted composite truss structure, provides a load path with high stiffness, mechanical attachment, and thermal separation between the Payload and spacecraft. The SM attaches outside the CIM with its aft end integrating directly to the bus. The spacecraft maintains an attitude off M1's boresight with respect to the Sun line to facilitate the <45 K thermal environment. SALTUS will reside in a Sun-Earth halo L2 orbit with a maximum Earth slant range of 1.8 million km, thereby reducing orbit transfer delta-v. The instantaneous field of regard provides two continuous 20 deg viewing zones around the ecliptic poles, resulting in full sky coverage in 6 months.

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**Keywords:** SALTUS; spacecraft; space observatory; mission architecture; deployable; sunshield

Paper 24071SS received May 15, 2024; revised Jul. 1, 2024; accepted Jul. 17, 2024; published Aug. 22, 2024.

J. Astron. Telesc. Instrum. Syst.

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# 1 Introduction

Northrop Grumman has developed an observatory concept and mission design for the Single Aperture Large Telescope for Universe Studies (SALTUS) that, if selected, would launch in 2032 for a 5-year baseline mission duration in a Sun–Earth halo *L*2 orbit. SALTUS will study a wide range of astrophysical objects, such as the youngest galaxies, protoplanetary disks, and a variety of solar system objects including planets, moons, Kuiper Belt objects, comets, and more. These studies will probe formation and evolution to answer fundamental questions about our cosmic origins, addressing key science aligned with the 2020 Astrophysics Decadal Survey<sup>1</sup> and the 2013 Astrophysics Roadmap.<sup>2</sup> References 3–6 expand on the importance of SALTUS to the National Aeronautics and Space Administration (NASA) science objectives and provide detailed discussions of the SALTUS goals.

For the SALTUS observatory flight system, as shown in Fig. 1, Northrop Grumman draws from its significant NASA space mission heritage and has selected the Northrop Grumman LEOStar-3 product line as the primary spacecraft architecture coupled with a scaled GEOStar-3 primary structure<sup>7</sup> to host the SALTUS Payload. We define the "observatory" as the spacecraft and Payload architectures. The Payload consists of a suite of far-infrared spectroscopic instruments, the cold corrector module (CCM), the inflation control system (ICS), the sunshield module (SM), the warm instrument electronics module (WIM), and the primary reflector module (PRM). The primary instrument suite is comprised of (1) the High-Resolution Receiver (HiRX): a four-band, high sensitivity, high spectral resolution heterodyne receiver and (2) SAFARI-Lite: a four-band, high sensitivity, moderate resolution grating spectrometer. The PRM is made up of a deployable 14-m off-axis parabolic reflector by way of an inflatable membrane (M1); a deployable, segmented boom; and a truss. The SM is a truss-based cylinder with two deployable sunshield layers (stowed in a hub), with layer 1 being  $\sim 48.5 \text{ m} \times \sim 19.2 \text{ m} (\sim 931 \text{ m}^2)$  and layer 2 being  $\sim 50 \text{ m} \times \sim 20 \text{ m} (\sim 1000 \text{ m}^2)$ , and it facilitates the SALTUS cryogenic <45 K environment for the PRM, CCM, HiRX, and SAFARI-Lite. Specialized truss-based composite structures, including an instrument deck and core interface module (CIM), have been designed specifically to facilitate a requirement-derived mechanical and thermal interface between the Payload and the spacecraft. Northrop Grumman will leverage extensive heritage and experience from L'Garde, which will provide the 14-m M1, and from NeXolve and Redwire Space, which will provide the SM. In addition to SALTUS systems engineering, Northrop Grumman will provide mission management, safety and mission assurance (SMA), and additional resources to the Mission Operations Center (MOC; operated by Northrop Grumman at the PI-institution University of Arizona's Applied Research Building).

Although the Northrop Grumman spacecraft architecture is more than capable of meeting mission requirements (e.g., orbit, environment and duration, launch vehicle (LV) compatibility, communications), SALTUS instrument-unique requirements have driven several key technical

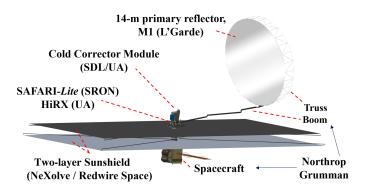


Fig. 1 SALTUS observatory. The partners listed are the University of Arizona (UA; PI-institution and responsible for HiRX), Space Dynamics Laboratory (SDL; Payload/CCM manager), SRON Netherlands Institute for Space Research (SAFARI-*Lite*), L'Garde (M1 primary reflector), and NeXolve and Redwire Space (sunshield module). Northrop Grumman provides mission management, SMA, and resources to the MOC and is responsible for the spacecraft and observatory architecture at large, including the composite instrument deck, CIM, ICS, deployable boom, and truss.

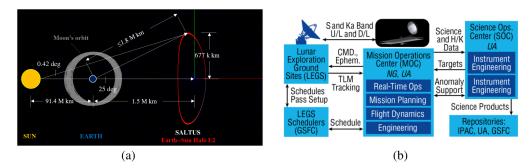
challenges associated with the observatory architecture, namely, (i) pointing stability (to allow the CCM to capture light from M1 and correct for wavefront error for diffraction-limited performance), (ii) thermal stability and control (to facilitate a stable M1 temperature < 45 K; a  $\Delta T \sim 250$  K over ~3 m between the "warm side" and "cryogenic side" of the observatory, separated by the sunshield), and (iii) lifetime, driven by a two-consumable system (first, sufficient propellant—for orbit transfer, station keeping, desaturation, and slew/settle times for observational efficiency, and second, sufficient inflatant gas (helium)—to maintain M1 inflation pressures that meet optical imaging performance). When coupled with the power of the corrective optics in the CCM and the performance offered by the Northrop Grumman spacecraft bus, the observatory architecture provides a robust solution for both the guaranteed time observation (GTO, ~30%) and the guest observer (GO, ~70%) Astrophysics Probe Explorer (APEX) mandated observing programs.

The outline of this paper is as follows. In Sec. 2, we describe the SALTUS mission implementation, including general requirements, mission traceability, launch, and orbit. Section 3 discusses the observatory design and the flight system. In Sec. 4, we expand in detail on the sunshield module design. Finally, Sec. 5 details the SALTUS lifetime, constrained by the propellant and inflation control systems, and discusses observational efficiency, momentum unloading, and the effects of micrometeoroids (MMs) on M1.

# 2 Mission Implementation

## 2.1 Concept Description and Mission Traceability

With a launch readiness date (LRD) no later than July 2032, SALTUS launches from Kennedy Space Center (KSC) with a launch energy (C3) of  $-0.6 \text{ km}^2/\text{s}^2$ . The launch is followed by a 2-month commissioning and orbit transfer phase that includes multiple delta-v ( $\Delta V$ ) burns to achieve a trajectory toward the destination Sun-Earth halo L2 orbit. Following HiRX and SAFARI-Lite instrument commissioning, SALTUS begins its 5-year baseline primary mission. Figure 2(a) illustrates the orbit's maximum 1.8 million km slant range from the Earth with a maximum 25 deg Sun-spacecraft-Earth angle chosen to simplify the orbit design, thus reducing the required orbit transfer  $\Delta V$ . Earth eclipses are avoided with minimal  $\Delta V$ , and the halo orbit is sized as such. The spacecraft attitude keeps the Sun at  $\sim 90$  deg off the observatory boresight and limits rotation to  $\pm 20$  deg of pitch and  $\pm 5$  deg of roll—this is critical for maintaining the <45 K cryogenic environment on the M1 side of the sunshield, and this orientation is maintained throughout the entire mission lifetime. Navigation requirements are easily met via Lunar Exploration Ground Sites (LEGS) ranging, in which data volume and required data rates result in a communication system that fits within bandwidth limitations, as discussed in Sec. 3. Operations require a weekly total ground contact of 7 h, with the science team generating the target list well in advance of the contact. This can be adjusted in phase A if necessary. The mission operations concept architecture is shown in Fig. 2(b).



**Fig. 2** (a) SALTUS Sun–Earth halo *L*2 orbit. The orbit has been sized such that Earth eclipses are avoided with minimal  $\Delta V$ . The Moon's orbit is shown for scale. (b) SALTUS mission operations architecture, jointly supported by Northrop Grumman and the University of Arizona's Mission Operations Center (MOC), Science Operations Center (SOC), and the Lunar Exploration Ground Sites (LEGS).

Mission design requirements	Spacecraft requirements	Ground system requirements	Operations requirements
- Orbit: Sun- Earth halo L2	- Propellant and inflatant to support a 5-year mission (Sec. 5)	- Compatible with LEGS ranging (Sec. 3.2.6)	- Transfer to L2
- 5-year mission duration	<ul> <li>Perform station keeping and desaturation to maintain observing efficiency (Sec. 5)</li> </ul>	- Archive science and housekeeping data (Sec. 3.2.4)	<ul> <li>Plan station-keeping maneuvers as needed—plan timing of science targeting,</li> </ul>
<ul> <li>Compatible with LV per AO guidance</li> </ul>	- Pointing knowledge: 3.3 arcsec, 1 $\sigma$		comm events, desaturation, calibrations, etc.
AO guidance	- Pointing accuracy: 10 arcsec, 1 $\sigma$		- Predict wheel momentum growth and plan desaturation
- Launch NLT July 2032	- Pointing stability: 0.66 arcsec, $3\sigma$ (over 10 min) (Sec. 3.2.7)		maneuvers
	- Temperature for Payload systems: <45 K (cryo side) (Sec. 3.2.8)		- Sun remains at 90 deg $\pm$ 20 deg of the observatory boresight and in the $-Z$ direction
	- Closed loop control of inflation to 5.1 Pa $\pm$ 5.1 $$ mPa (Sec. 5)		
	- LEGS compatibility (Sec. 3.2.6)		

Table 1 Summary overview of SALTUS mission rec	juirements.
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The SALTUS instantaneous field of regard (iFOR) is a circumpolar band of 40 deg width in the ecliptic frame, resulting in two continuous viewing zones of 20 deg around the ecliptic poles and full sky coverage in 6 months. This coverage is possible based on the attitude capabilities outlined above, coupled with the ability of the spacecraft to rotate 360 deg around the Sun line. The propulsion system performs momentum desaturation and station-keeping maneuvers periodically throughout the mission, as described in Sec. 5. The overall SALTUS pointing approach combines the spacecraft attitude determination and control system (ADCS) and the fast-steering mirror on the CCM. The spacecraft is required to point the CCM within 60 arcsec of its intended target, which is well within the scan range of the CCM's fast-steering mirror. Generally, targets outside the solar system are effectively inertially fixed and are treated as such for ADCS sizing. The process is repeated via stored command for moving solar system targets. Once a target is acquired, the observatory must have <0.5 arcsec pointing stability over a 20-s period in between fast-steering mirror adjustments. The pointing stability requirement is an allocation of the overall transfer efficiency budget for the CCM. Note that the CCM transfer efficiency accounts for factors that ultimately determine the photon flux at each of the detectors. See Ref. 8 for CCM capabilities and optical performance.

Because the availability of targets varies seasonally, with some periods of the mission more target-rich than others, the observation time requirement flows down to a conservative allocation of 60% operational target efficiency as discussed in Sec. 5.<sup>3</sup> Table 1 shows a summary version of the SALTUS mission traceability matrix (MTM), which includes the mission design requirements, spacecraft requirements, ground system requirements, and operation requirements. We include references in parenthesis to sections in this paper where spacecraft and ground system requirements are addressed in detail.

#### 2.2 Launch, Orbit, and Basic Operations

SALTUS will launch on a "Performance Upper (Std. PLF)" NASA-provided LV and will perform orbit transfer to the Sun–Earth L2 Lagrange point. This orbit was chosen for a variety of reasons, including no Earth/Moon eclipses, good stray light conditions, good thermal stability conditions, minimal  $\Delta V$  station keeping, and the potential for enabling scientific synergy with the James Webb Space Telescope (JWST) and other missions. We conducted a launch window analysis to offer a wide number of launch opportunities based on determining an optimal transfer trajectory design from an Earth departure asymptote to the desired halo orbit using GMAT—General

Event	ΔV
Trajectory correction maneuver (TCM) 1	25.0 m/s
Mid-course correction (MCC)	66.4 m/s
TCMs 2 to 4	50.0 m/s
Halo insertion	17.1 m/s
Station-keeping (for 5 years)	14.8 m/s
Total	173.4 m/s
Contingency	30%
Total (incl. contingency)	225.4 m/s

Table 2 SALTUS	$\Delta V$ budget.
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Mission Analysis Tool.<sup>9</sup> We considered a launch window every day for 1 year from the LRD on July 1, 2032, to June 30, 2033. Launch inclinations not accessible from KSC were discarded. In addition, we removed cases in which the required maneuvers (including mid-course correction (MCC) plus halo insertion) had a  $\Delta V > 55$  m/s or a C3 > -0.6 km<sup>2</sup>/s<sup>2</sup>. Our analysis yielded 104 viable launch windows that met these criteria between July 7, 2032, and December 29, 2032. This  $\Delta V$  budget is shown in Table 2 reflecting the 5-year baseline mission duration.

Following launch (L + 0 days) and LV separation, the observatory autonomously deploys its solar array and enters a stable Sun-pointed mode. The operations team performs an initial checkout in preparation for an LV trajectory correction burn within the first 3 days after launch. The orbit transfer consists of the LV trajectory burn, an MCC maneuver  $\sim L + 44$  days (resulting in a coincident trajectory with a stable low-energy transfer), and finally, an injection burn L + 107days to place the observatory in the destination Sun–Earth halo L2 orbit. Trajectory correction maneuvers (TCM) are performed as needed during the transfer with LEGS ranging providing requisite orbit knowledge to support the transfer. The start of instrument commissioning does not commence until  $\sim L + 151$  days and is immediately followed by science operations, baselined at  $\sim L + 167$  days. The orbit meets its Sun-spacecraft-Earth angle and maximum range requirements at 25 deg and 1.8 million km, respectively. Figure 3 depicts the orbit transfer and mission timeline graphically with appropriate labeling.

Instrument commissioning is executed after several observatory subsystem deployments primarily, PRM and SM deployments after the CCM has sufficiently cooled to allow cryocooler

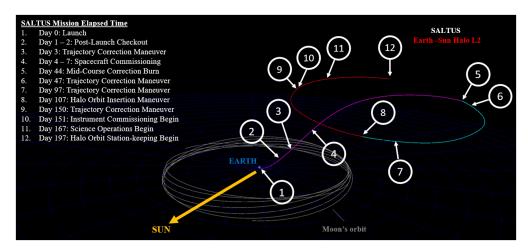


Fig. 3 SALTUS launch into a Sun–Earth halo *L*2 orbit annotated with maneuvers and sequence of activities to prepare for science operations. The Moon's orbit is shown for scale.

operation. The PRM and SM are not deployed until all TCMs have been completed-this avoids excessive torque on the observatory during maneuvers, corrections, or insertion, in which the observatory only undergoes station keeping after full deployment. Nominal operations consist of repeated activities, as follows: (i) observing science targets (a typical observation of  $\sim 5$  h each), (ii) momentum desaturation, and (iii) slewing (including settling time) to the next target based on the concept of operations (CONOP) for GTO and/or GO programs. M1 is under active inflation control during an observation to meet optical imaging performance, in which inflation pressures are increased to 5.1 Pa  $\pm$  5.1 mPa to meet this performance just prior to observation onset. A detailed description of the inflation scheme, designed to maximize/extend SALTUS lifetime by only consuming inflatant gas during science data collection is outlined in Ref. 10. Throughout a week of operations, the observatory slews to point its high-gain antenna (HGA) toward the Earth to perform ground contact (total 7 h per week, appropriately distributed via science CONOP) of high-rate Ka-band data downlink and command uplink followed by low-rate S-band (low-bandwidth) LEGS ranging. An additional 7 h per week of S-band coverage has been budgeted for state-of-health (SOH) monitoring and will be optimized for efficiency and operational safety. Minor station keeping is scheduled every  $\sim 90$  days. We discuss the operational on-sky efficiency of SALTUS in Sec. 5.

Finally, we impose two relevant mission requirements for navigation operations. First, the observatory must avoid drifting away from *L*2, and second, the observatory must maintain communications. The link described above is sized to support simultaneous command, telemetry, and ranging, and we expect to perform LEGS ranging to these navigation-driven requirements. We also considered SM-induced orbital perturbation by assessing solar radiation pressure (SRP). This analysis was carried out in GMAT with the model including a simple 1000 m<sup>2</sup> SRP plate perturbation. We found that the effect of SM SRP is <2 m/s over the entire mission duration and is captured in our  $\Delta V$  calculations in Table 2. We also included  $\Delta V$  from momentum unloading (MU), which we found to be ~0.03 m/s per day. Station keeping (for 5 years) includes station-keeping maneuvers to maintain the halo orbit and the above corrections due to MUs. From the frequency of ranging contacts (at least two per week) and the minor SM SRP perturbations and MU described here, the  $\Delta V$  requirements are shown to be modest. Therefore, the orbit drift is small, and a large impact on navigation performance is not expected. A detailed range accuracy requirement study will be completed in phase A.

# 3 Flight System Design

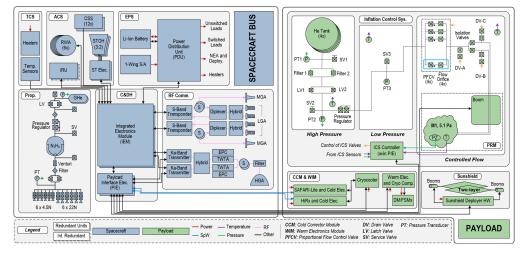
## 3.1 Overview

The SALTUS flight system is designed to meet the mission requirements outlined in Table 1 with margin while maximizing heritage and operational flexibility. The flight system is based on the Northrop Grumman LEOStar-3 product line, a platform with extensive heritage supporting successful NASA category 2 programs both in Earth science (e.g., JPSS-2, Landsat 9, ICESat-2) and astrophysics (e.g., FERMI, Swift). Current Northrop Grumman programs continue to develop and improve the platform. Due to observatory loads and volume, SALTUS packages the LEOStar-3 architecture within a scaled primary structure based on the GEOStar-3. Payload interfaces are well defined and accommodated with standard protocols. In this section, we expand on the spacecraft, the Payload and SM interfaces, and all key flight system subsystems. We also discuss the PRM as Northrop Grumman is responsible for PRM deployables. The ICS is described in Sec. 5 because it directly relates to mission lifetime, which is the focus of Sec. 5. We show a summary flight system block diagram in Fig. 4; the spacecraft stowed and deployed configurations in Fig. 5; summary of technical budgets in Table 3 (mass), Table 4 (data), Table 5 (power), and Table 6 (link); and a flight system margin summary in Table 7.

## 3.2 Spacecraft Bus and Subsystems

## 3.2.1 Structures

The GEOStar-3 structure and mechanical subsystem support the SALTUS Payload, provide the primary load path between the bus and LV, and the means of attachment for four required helium inflatant tanks for the ICS. The structure also supports the propulsion subsystem and



**Fig. 4** SALTUS flight system block diagram. The legend indicates selectively redundant or internally redundant components. The LEOStar-3 Integrated Electronics Module (IEM) avionics is coupled with a Payload Interface Electronics (PIE) module to meet SALTUS science and mission requirements. Both the inflation control system (ICS) and sunshield module (SM), as well as the cold corrector module (CCM), warm instrument electronics module (WIM), and primary reflector module (PRM), are captured under the Payload. The ICS includes four tanks (helium gas) mounted externally to the GEOStar-3 primary structure. The CCM resides in the cryogenic environment (M1 side, < 45 K), whereas the WIM resides inside the bus structure in the warm environment for thermal considerations (spacecraft side, ~310 K).

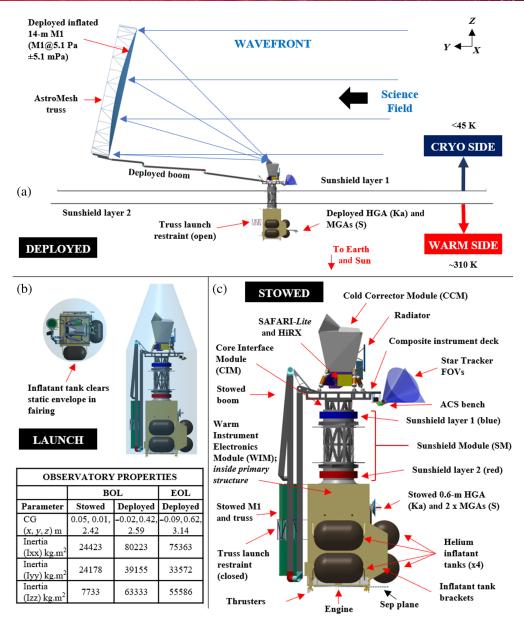
provides ample mounting locations and radiative surfaces for the flight system and Payload components. At the aft end, a heritage launch adaptor facilitates the interface between the space-craft and LV.

# 3.2.2 Spacecraft to payload interface

A fully composite truss-based structure—the CIM—provides the means of mechanical attachment and thermal separation between the Payload and spacecraft, as shown in Fig. 5(c). This truss structure is based on JWST heritage and is tuned to be near zero coefficient of thermal expansion (CTE) in the cryogenic environment (see Sec. 3.2.8 regarding thermal stability). The CIM not only provides launch load capabilities and on-orbit thermal stability but also includes accessibility during integration and testing (I&T) activities to route and thermally isolate the multiple cables and lines that span the spacecraft and Payload. On top of the CIM, we designed a truss-based instrument deck leveraging similar JWST heritage and materials. The instrument deck provides the primary mechanical means of attachment for the CCM, ACS bench, and deployable PRM. Similar to the CIM, it is also tuned to near zero CTE at cryogenic temperatures to ensure thermal stability and minimize pointing errors to meet pointing requirements. The SM is also a part of the SALTUS Payload and was designed to interface directly with the CIM and spacecraft maintaining an ideal load path with high stiffness and thermal performance.

# 3.2.3 Propulsion

The propulsion subsystem performs all maneuvers to reach the Sun–Earth halo L2 orbit as well as MUs and orbit maintenance throughout the mission. The subsystem is a mono-propellant hydrazine system sized to 1093.7 kg maximum expected value (MEV) with 5.8 kg MEV of pressurant based on flight-proven components. Six 22 N  $\Delta V$  thrusters perform all impulsive maneuvers as well as X/Y attitude control during these maneuvers. Six 5 N ACS thrusters operate for Z-axis control during impulsive maneuvers and for MUs. All thrusters mount on the aft end of the spacecraft bus with the  $\Delta V$  thrusters oriented to provide thrust along the +Z-axis and ACS thrusters oriented to provide attitude control in all three axes. The propellant budget utilizes the MEV launch mass,  $3\sigma$  low thruster performance, and maturity-based contingencies as well as



**Fig. 5** (a) SALTUS deployed configuration. The "warm side" is Earth and Sun facing. M1 boresight is ~90 deg ( $\pm$ 20 deg pitch,  $\pm$ 5 deg roll) to the Sun line, and the *Z*-axis can rotate 360 deg around this line. (b) SALTUS launch configuration. The observatory fits in the static envelope of the LV fairing. We also show the observatory center of gravity (CG) with respect to the spacecraft origin at the separation plane ("Sep plane") and inertia in stowed and deployed configurations. (c) SALTUS stowed configuration. Sunshield layers are colored to indicate layer 1 (blue, cryo side) and layer 2 (red, warm side).

efficiency factors such as misalignments, flight dynamics errors (relating to  $\Delta V$  requirement uncertainty), and residual fuel.

# 3.2.4 Command and data handling

The command and data handling (C&DH) subsystem provides command, control, and data handling capabilities within the SALTUS flight system via block-redundant integrated electronic modules (IEMs) and block-redundant Payload interface electronics (PIEs). The IEM handles all core command, control, and data handling capabilities and provides triple modular redundancy (TMR) storage for the spacecraft and Payload SOH data storage, providing ample data

Mass element	CBE (kg) (1)	Contgy. (%)	MEV (kg) (2)
Spacecraft	2090.0	10.2	2304.0
Payload	939.8	20.8	1135.6
Total observatory dry mass	3029.8	13.5	3439.6
LV performance to $C3 = -0.6 \text{ kg}^2/\text{s}^2$			6846.0
Helium inflatant			200.0
Hydrazine propellant			1093.7
Pressurant			5.8
Total observatory wet mass (3)			4739.1

# Table 3 SALTUS mass budget summary.

(1) Current best estimate. (2) Maximum expected value. (3) Total observatory wet mass margin (including contingency) to LV performance is  ${\sim}45\%$ ; see Table 7 margin summary.

## Table 4 SALTUS data budget summary.

Parameter	Value
Data rates	
SAFARI-Lite science data rate (kbps)	300.0
HiRX science data rate (kbps)	250.0
Bounding science data rate (kbps)	300.0
Spacecraft SOH data rate (kbps)	7.7
Instrument HK data rate (kbps)	0.3
Total SOH data rate (kbps)	8.0
Data storage	
Time between data downlinks (days)	7.0
Science data to store (Gbit)	181.6
Science data storage available in PIE (Gbit)	384.0
Science data storage margin (%)	112.0
SOH data to store (Gbit)	4.8
SOH data storage available in IEM (Gbit)	21.0
SOH data store margin (%)	334.0
Data downlink	
St. data vol. to downlink, Sci + SOH (Gbit)	186.3
Downlink information rate (kbps)	10,000
Allocated time to downlink (h)	7.0
Downlink volume capacity (Gbit)	252.0
Downlink volume margin (%)	35.0

	Scien	ce + DL	(HiRX)	_	cience + AFARI- <i>L</i>		Orbit	average	power
Subsystem	CBE (W)	Contgy. (%)	MEV (W)	CBE (W)	Contgy. (%)	MEV (W)	CBE (W)	Contgy. (%)	MEV (W)
Bus total	921.5	9.6	1010.4	925.0	9.8	1015.6	917.6	9.5	1005.0
Payload total	730.4	19.5	872.9	845.9	23.5	1045.1	732.5	19.8	877.5
Observatory total	1651.9	14.0	1883.3	1770.9	16.4	2060.6	1650.1	14.1	1882.5
Observatory total + 30% margin	2147.5	14.0	2448.3	2302.1	16.4	2678.8	2145.1	14.1	2447.2
Solar array sizing mode considerations						Contg	ıy. (%)		
Solar array margin at EOL for array sizing case with downlink (1)							20	).0	
Solar array margin at EOL for array sizing case without downlink (2)							39	9.0	
Solar array margin at EOL during slew (3)							8	.0	
Solar array margin at EOL during momentum unload (3)						38	3.0		

## Table 5 SALTUS power budget summary.

The driving steady-state power mode is a SAFARI-*Lite* science observation with HiRX in stand-by with a simultaneous Ka-band science data downlink (DL). (1) With a maximum MU duration of ~4 min and considering MU and slew battery recharge. This sizing case assumes a nominal observation and a continuous 5 h science data DL. (2) The nominal DL cadence of 7 h per week; science + DL is used as a conservative case. Assuming a return to an observation without DL, the solar array has an additional margin when considering battery recharge demand and correcting MU duration. (3) We assume that MU and slew modes draw power from the battery to avoid sizing the solar array to infrequent modes (4× per day). These modes could both be powered by the solar array.

	Low-r	rate/safe	Т	T&C	Science
Parameter	Uplink	Downlink	Uplink	Downlink	Downlink
Frequency (MHz)	2072.5	2287.5	2072.5	2287.5	26,375.0
Elevation angle (deg)	5	5	5	5	5
Maximum range (km)			1,900,000		
Information rate (kbps)	1.0	1.0	2.0	8.0	10,000.0
FEC (1)	None	C + RS	None	C + RS	<i>C</i> + RS
Bit rate (kbps)	2.0	2.3	2.0	18.3	22,870.0
Modulation	BPSK	BPSK	BPSK	BPSK	QPSK
Antenna coverage	80%	80%	50%	MGA	HGA
Spacecraft EIRP (dBm)	N/A	38.3	N/A	52.8	88.0
Spacecraft G/T (dB/K)	-33.9	N/A	-30.8	N/A	N/A
Ground station			LEGS		
BER			$1 \times 10^{-6}$		
Link margin (dB) (2)	6.8	3.2	6.9	8.6	5.0

#### Table 6 SALTUS link budget summary.

(1) C + RS represents convolutional + RS (255, 223). (2) Margin for TT&C link maintained at a minimum of 6 dB for ranging-induced losses. All other links are maintained at a minimum of 3 dB.

Parameter	Requirement	Performance	Margin
Observatory wet mass	4739.1 kg	6846.0 kg (1)	45%
Observatory dry mass	3439.6 kg (2)	5204.1 kg (3)	43%
Propellant tank capacity	1093.7 kg	1641.9 kg	50%
Solar array performance (EOL)	2211.0 W	2874.9 W	30%
Battery capacity (BOL)	96.0 A-h	134.0 A-h	40%
Pointing accuracy $[1 \sigma]$	10.0 in.	1.2 in.	736%
Pointing stability $[1 \sigma]$	2.0 in.	0.66 in.	189%
Pointing knowledge $[1 \sigma]$	3.33 in.	1.19 in.	180%
Science data storage	181.6 Gb	384.0 Gb	112%
Link margin   TT&C uplink	0 dB	6.9 dB	6.9 dB
Link margin   TT&C downlink	0 dB	8.6 dB	8.6 dB
Link margin   Ka-band downlink	0 dB	5.0 dB	5.0 dB

 Table 7
 SALTUS flight system margin summary.

(1) LV performance capability to SALTUS orbit. (2) Includes full inflatant load of 200 kg. (3) Maximum dry mass assuming a full propellant tank.

storage margin. The IEM is augmented with block-redundant PIE units that provide command and telemetry interfaces for each element of the Payload and to the redundant Ka-band system for the downlink of stored SOH and science data. The PIE also provides the ICS controller functionality, monitoring analog telemetry from the ICS and maintaining pressure within M1. In addition, the PIE contains sufficient flash storage with TMR capability for science data storage. This storage capability provides ample margin for science data, as shown in Table 4. The SALTUS PIE is derived from similar units flown on Landsat 9 and JPSS-2 that provided mission-unique functionalities to their respective Payloads and redundant interfaces to the IEM.

# 3.2.5 Power

The electrical power subsystem (EPS) supplies power to the spacecraft and Payload and consists of a single deployable, non-articulating solar array wing with a power distribution control, charging unit (PDU), and a Li-ion battery. Figure 4 expands on this architecture, Table 5 summarizes the power budget for driving steady-state modes, and Table 7 includes the solar array and battery performance. The battery is sized to support  $\Delta V$  maneuvers within the allowed depth of discharge (DOD), accounting for all battery usage efficiency factors as well as capacity fading at EOL. The battery provides a greater margin to all other battery-powered modes. The solar array supports all mission phases and modes with margin, and solar cell efficiency losses for the expected 100°C operating temperatures have been captured. Sized for a maximum Sun angle of 25 deg off the solar array surface normal (per Fig. 2), the non-articulating solar array permits pointing across the entire SALTUS FOR. The driving steady-state power mode is a SAFARI-*Lite* science observation with HiRX in stand-by with a simultaneous Ka-band science data downlink. The solar array provides a greater margin to all other steady-state mission modes. As a conservative approach, MU and slew modes are on battery power because the solar array is not gimbaled but both could be powered by the solar array, if necessary, as noted in Table 5.

## 3.2.6 Telecommunications

The telecommunication subsystem provides both low-rate tracking, telemetry, and commanding (TT&C) capabilities throughout all SALTUS mission phases and high-rate science data downlink capabilities and as a result requires two distinct systems: a low-rate S-band system and a high-rate Ka-band system, as shown in Table 6.

The S-band system is designed for compatibility with select ground and space assets during Launch and Early Orbit Phases (LEOPS) and the NASA Near Space Network LEGS network during cruise and science phases. A pair of low-gain, quadrifilar helix antennas (LGAs) mount onto opposite sides of the spacecraft bus, providing near  $4\pi$ -steradian coverage during uplink and downlink. Both S-band receivers remain powered throughout all flight system modes, whereas the active S-band transmitter is powered only during post-separation and rate capture, safe mode, and scheduled passes. Each S-band channel is augmented with a medium-gain, monofilar antenna (MGA) that points in the same direction as the 0.6-m Ka-band high-gain antenna (HGA) to provide a higher rate S-band capability for TT&C during science data downlink.

The Ka-band system is compatible with the LEGS network for science data downlink and draws heritage from the JPSS-2 mission. The PIE and Ka-band transmitters modulate and condition the data stream for downlink to LEGS. The body-fixed HGA has a beamwidth greater than the angular size of the Earth at the Sun–Earth halo L2 orbit and points in the aft direction. The HGA and MGAs are stowed against the spacecraft bus during launch and are boom-deployed during the cruise phase. Throughout a period of 1 week (optimized via CONOP), SALTUS points its HGA toward the Earth to perform ground contact of 7 h total high-rate Ka-band data downlink and command uplink followed by low-bandwidth, low-rate S-band via LEGS ranging. As noted in Sec. 2.2, an additional 7 h per week of S-band coverage has been baselined for SOH monitoring and other communications as required by mission needs.

#### 3.2.7 Attitude control

The ACS provides pointing stability, control, and knowledge for science observation while providing sufficient agility across the FOR. SALTUS pointing requirements (as shown in Table 1) are readily met with margin on the LEOStar-3 platform as a result of carefully selected star trackers (STs), inertial reference units (IRUs), reaction wheel assembles (RWAs), and Northrop Grumman flight-proven algorithms (e.g., ICESat-2, Landsat 8/9). We show the ACS bench location and approximate ST FOVs in Fig. 5 and provide performance margins for each ACS mode in Table 7. Attitude stability and control are maintained and stabilized throughout all mission phases, beginning with LV separation. During  $\Delta V$  maneuvers, the ACS utilizes its  $\Delta V$  mode providing slew capability to and from the maneuver attitude. In spacecraft safe mode, the ACS nulls spacecraft rates and points the -Z axis at the Sun while keeping the solar array Sun pointed with a slow roll induced about the Z axis. Safe mode therefore maintains a power-positive, thermally safe, commandable attitude that avoids SALTUS pointing constraints. This effectively eliminates solar pressure-induced momentum accumulation and keeps the spacecraft approximately Earth-pointed as well.

Attitude sensor and CCM misalignments are minimized by collocating the dedicated, thermally controlled ACS bench with the CCM on the instrument deck, and the ACS sensors are oriented to provide attitude knowledge in all three degrees of freedom (DoF). Six RWAs manage momentum and slew the observatory, and the six 5 N ACS thrusters provide MU as needed. SRP, driven by the sunshield area (see Sec. 4), dominates the environmental torques during science operations and remains nearly constant during observation. Current predictions of environmental torques acting on the SALTUS observatory require an MU event every 5.4 to 8.0 h (BOL–EOL). A typical science observation is estimated to be ~5 h, and because contiguous observations are not a requirement, this MU cadence is acceptable. We discuss MU in greater detail in Sec. 5.

The LEOStar-3 platform has extensive heritage providing arcsecond-level precision-pointing and pointing stability capabilities and readily meets the SALTUS pointing requirements with margin. Using Northrop Grumman's flight-validated simulation capabilities for attitude estimation and control errors and allocations based on heritage programs, the predicted performance of the flight system ACS meets SALTUS needs with a robust margin, as shown in Table 7.

## 3.2.8 Thermal control

**Overview.** The thermal control subsystem (TCS) employs a passive, cold-biased design with radiative cooling and heaters to keep SALTUS flight system components within acceptable temperature limits during all operational mission modes. As noted previously, the +Z side of

the observatory faces away from the Sun during science observations (in fact, once the cryogenic environment has been established, +Z will maintain this attitude until EOL  $\pm$  margin in roll, pitch, and yaw), providing a thermally stable environment and ample exterior radiator area. Radiators and heaters are sized to provide a large margin against qualification temperatures, and all heaters are sized with appropriate duty cycles under worst-case cold and low-voltage conditions.

The SALTUS spacecraft is located on the Sun-side of the SM, as shown in Fig. 5(a). As a result of the large sunshield area, this configuration causes the external surfaces of the spacecraft to be subjected to high amounts of (i) sunlight reflected off the deployed SM and (ii) IR-back-loading (radiant heat) emitted from the deployed SM surfaces that are in-view of spacecraft surfaces. The magnitude of these impacts on spacecraft and SM thermal performance can vary significantly depending upon the size, configuration, and external coatings of the deployed SM; the configuration of the spacecraft; and the interfacing geometry and hardware configuration between the two. Consequently, early thermal and mechanical design efforts have considered interface designs between the spacecraft and SM via the CIM (details discussed in Sec. 3.2.2), and bus operating temperatures have been captured when selecting components and calculating operating efficiencies.

Fortuitously, the JWST design team encountered similar interface considerations for its spacecraft and sunshield. In the JWST case, thermal design necessitated the inclusion of deployable radiator shields (DRS) and fixed radiator shields (or non-deployable radiator shields, FRS). Specialized insulation, coating designs, and lightweight structures resulted in a highly efficient solution, not only in its deployed (in-flight) state but also in stow. The DRS provided valuable functionality by covering radiators to reduce spacecraft heat rejection capability, thus reducing heater power for the stowed configuration when less power is available (prior to solar array deployment). In phase A, Northrop Grumman will leverage this significant domain knowledge from this JWST-proven concept to guide an efficient, robust, and low-risk SALTUS thermal interface design to address the warm side bus thermal design challenges in full.

*Thermal environments.* The observatory has two distinct thermal zones: (i) the warm side on the -Z side of the sunshield and (ii) the cryogenic side on the +Z side of the sunshield, as shown in Fig. 5(a). Notably, for thermal concerns, the warm side contains the WIM and solar array, whereas the cryogenic side contains the CCM, PRM, and ACS bench. As discussed in Sec. 3.2.2, these environments are mechanically and electrically connected via the CIM. Using the same analytical tools as JWST, we predict an equilibrium temperature of  $\sim 310$  K on the warm side, with radiative cooling to deep space allowing all components on the cryogenic side to cool to  $\leq$ 45 K. This is critical for the exceptional IR sensitivity for SALTUS science. To fully understand the stepdown in temperature from ~310 to ≤45 K, we constructed a cryogenic heat map of SALTUS as shown in Fig. 6. The HiRX and SAFARI-Lite focal planes require cooling to ~5.25 K; therefore, we selected a build-to-print version of the JWST MIRI cryocooler to provide 31 mW of lift at 5.25 K, plus 110 mW of lift at 20 K for the SAFARI-Lite low-noise amplifiers (LNAs). This performance includes a > 30% margin. We used thermal desktop modeling to ensure that the CCM's design provided 500 mW of cooling at 45 K and included two side-looking radiators,  $1.5 \text{ m}^2$  and  $0.5 \text{ m}^2$ , respectively, to provide additional radiative cooling needs for HiRX. The MIRI compressor system resides on the warm side of the spacecraft (for thermal isolation) and is coupled to the WIM, where gas lines facilitate the pressurized helium to a valve at the 5.25 K stage of the system on the cryogenic side via the CIM. Northrop Grumman has extensive experience with the MIRI cryocooler and therefore understands its power consumption well. Thus, a 2.7 m<sup>2</sup> radiator (coated with specialized paint) radiates to deep space to cool the WIM. In addition, the instrument radiator 4  $m^2$  surface area provides a 50% margin on these loads and will be placed orthogonally to the spacecraft-Sun axis for a clear view of deep space. All radiator sizing in this work is a first-order approximation and will be refined and fully addressed in phase A.

**ACS bench.** The ACS bench, a thermally controlled deck, contains three STs and an IRU, as shown in Fig. 5(c). The bench is mounted on the underside of the composite instrument deck via titanium flexures for conductive isolation. Importantly, the ACS bench is completely out of the

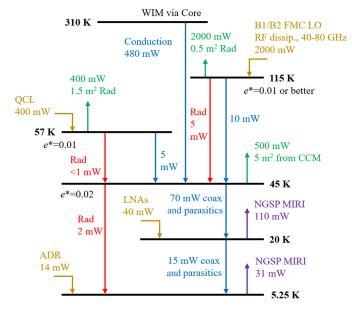


Fig. 6 SALTUS cryogenic heat map. Acronyms in the figure: ADR, adiabatic demagnetization refrigerator; CCM, cold corrector module; LNA, low-noise amplifier; LO, local oscillator; QCL, quantum cascade laser; WIM, warm instrument module.

M1 and CCM cryogenic FOVs and draws heritage from an identical ICESat-2 design. The STs and IRU take advantage of two dedicated radiators allowing each to radiate heat to space—one sized to compensate for ~1 W per ST, and the other sized for the IRU's ~40 W at 20 C. Because the STs and IRU are used in all ACS modes, survival heaters maintain greater than qualification temperatures in the event of an anomaly. In addition, ST and IRU blankets surround the units, minimizing instrument deck radiative coupling. Utilizing this design as well as ICESat-2 heritage meant that additional qualification to cryogenic ACS operating temperatures could be avoided. A detailed flexure/MLI design will occur in phase A.

**Sunshield module.** Because the SM allows direct radiative coupling between the warm side (spacecraft) and cryo side (Payload), other thermal control features are designed into the interface between the CIM and SM. Single- and multiple-layer radiative barriers (i.e., blankets placed near the top and bottom of the SM) are planned to eliminate radiative coupling with no impact on the design. Cable and harness traversing the warm to cryogenic environments will be flat and have high emittance wrapping to enhance thermal radiation. If needed, a harness radiator will be added.

For the harness in the CIM region, conductors, shielding, and insulation will be chosen to minimize conducted heat. An environmental shield limits radiative view factors of the warm CIM to the cryocooler refrigerant line, lowering radiative coupling and the possibility of icing.

The thermal effects of the SM on the spacecraft and solar array are also considered. We used JWST flight actuals and found these data relevant due to similar sizing, space, and radiative coupling. We used the JWST peak observed operating temperature on the solar array as the nominal SALTUS case and sized the SALTUS single-wing solar array on that basis. Temperatures of thermally isolated hardware, such as the boom, are driven by radiation that changes little over the SALTUS iFOR.<sup>10</sup> Therefore, material CTE matching in the composite boom was also considered. The boom has aluminum and titanium fittings, which have a positive CTE. The composite's CTE is slightly negative and can be tuned to make the net boom CTE near zero over the relevant M1 temperature range. Even when the CTEs are tuned, the ability to perfectly match them is limited by the finite precision of CTE measurement, roughly 0.01 ppm/ measurement. Because there are three materials, the minimum CTE would be  $\sqrt{3}$  times this value or ~0.02 ppm. For a ~17-m boom and the maximum temperature change of 1 K, say, the boom would change length less than 0.5  $\mu$ m, which can be corrected by the optical system.

## **3.2.9** Flight software and in-flight fault management

Nearly all functionality required for SALTUS is already part of the baseline LEOStar-3 C&DH and ACS flight software (FSW). This FSW has a proven flight track record from missions such as ICESat-2, Landsat 8/9, and JPSS-2, where SALTUS can leverage extensive re-use of existing FSW with modifications limited to SALTUS-unique functions. This setup offers modularity and flexibility for additional features/capabilities in which reconfiguration is accessible on-orbit.

Redundancy via in-flight fault management is implemented throughout all subsystems, where standard single-point failure exemptions are acceptable for structure, fuel lines, tanks, and the HGA. Onboard fault detection via FSW as the primary and hardware as the secondary detects and responds to anomalous conditions as identified. Flexible, heritage FSW TLM monitoring (TMON) is used to manage onboard fault detection and correction with the list of critical TLM mission configurables. The FSW maintains a list of failure symptoms for each component. If TLM violates both the threshold and persistence check, the FSW TMON function responds by executing the appropriate command sequence. As noted previously, safe mode sheds all non-critical loads and achieves Sun pointing using the CSSs, and both S-band receivers are always on. Returning SALTUS to science operations is performed by the mission operations staff on the ground.

## 3.3 Primary Reflector Module (PRM)

#### 3.3.1 Overview

The SALTUS PRM is made up of three key components: the 14-m M1, the AstroMesh segmented boom, and the AstroMesh truss. The L'Garde M1 membrane is discussed in detail in Ref. 10. This section will focus on the AstroMesh boom and truss, which Northrop Grumman is responsible for in this development.

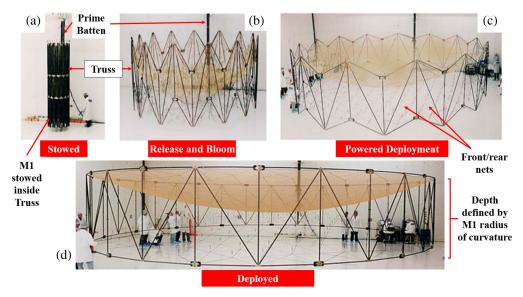
The AstroMesh reflector was developed in the late 1990s<sup>11</sup> for the Thuraya constellation and has been refined over the last 30 years with over eleven successful mission deployments (see Table 8). The AstroMesh architecture is therefore well proven and inherently reliable and offers robust deployment kinematics for a wide range of applications. The AstroMesh truss is designed as an efficient drum-like structure with high deployed stiffness, extremely low mass, and high thermal stability, making it a desirable option for the SALTUS use case. Indeed, its high structural stiffness allows for deployed performance measurements in 1G environments, further enhancing I&T capabilities. Crucially, the architecture was designed with scaling in mind, in which an increase in truss outer diameter (aperture size) is implemented without significant change, thus maintaining the heritage and minimizing mission-unique development.

The basic AstroMesh architecture as shown in Fig. 7 consists of a flat perimeter truss that supports front and rear nets made of high-precision composite tension "webs," which define a

Parameter	SMAP	Inmarsat-4	Inmarsat-6	Alpha sat	Thuraya	MB Sat	SALTUS
Aperture size	6 m	9 m	9 m	11 m	12 m	12 m	14 m (1)
Flown in space	Yes	Yes	Yes	Yes	Yes	Yes	-
#Successful deployments	1	3	2	1	3	1	-
f/D (2)		1.24					
ESD/PIM (3)		Compliant: V	erified by de	sign and de	emonstrate	ed	Verif. by design
Aperture deployment	Offset						Offset
Reflector mass (4)	29 kg	49 kg	49 kg	63.5 kg	63.5 kg	63.5 kg	12 kg (5)

#### Table 8 SALTUS AstroMesh truss and boom flight heritage.

(1) The main change for SALTUS is a scaling of the truss for 12-14 m. (2) Demonstrated in aperture size range. The SALTUS boom will be scaled for f/D. (3) AstroMesh is electrostatic damage (ESD) compliant and verified passive intermodulation (PIM)-free by design. (4) Driven by aperture, not mission unique. (5) Includes 20% contingency.



**Fig. 7** (a)–(d) SALTUS AstroMesh architecture showing the stowed and deployed configurations, as well as two key steps in the truss deployment: the release and bloom and the powered deployment. Note that the golden mesh reflective surface shown in this figure is illustrative only; the SALTUS M1 inflatable membrane will instead occupy this volume.

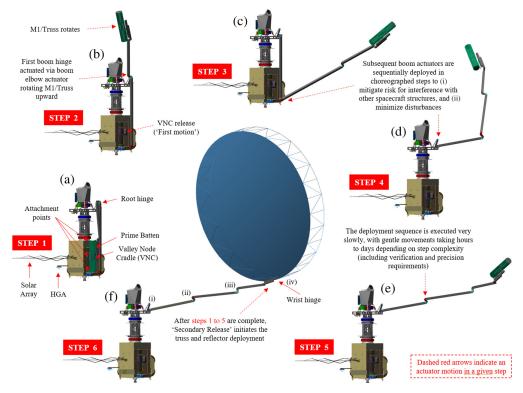
geodesic surface. The depth of the truss structure is defined by the reflector aperture and radius of curvature. Note that, for the SALTUS application, these webs will be used for structure only and are not needed to form the surface geometry of M1—this is driven solely by the ICS. Coupled with the truss are high-precision, high-heritage deployable booms, also scalable to meet increases in the truss diameter without impact on heritage. The AstroMesh truss and boom combination is fully electrostatic damage (ESD) compliant with a demonstrated passive intermodulation (PIM)-free design. The gold-molybdenum mesh shown in Figs. 7(b)-7(d) is normally used for RF applications and is included in the figure for illustrative purposes only.

## 3.3.2 Heritage and TRL

Table 8 highlights a range of space flight heritage missions that have successfully deployed the AstroMesh system. The SALTUS 14-m truss diameter is easily within the capabilities of the AstroMesh scalable design (as noted in Sec. 3.3.1) in which all previous missions shown in Table 8 have demonstrated f/D ratios in line with the expected SALTUS M1 f-number. Previously demonstrated offset (off-axis) aperture deployments and reflector masses also introduce no additional development for SALTUS given the extremely lightweight mass of the M1 membrane. Table 8 also highlights a heritage assessment for the truss and boom with an associated TRL-6 assigned to each component. We expect to comply with all partial heritage elements, with the key required changes identified as (i) a scaling of the truss from demonstrated 12-m to 14-m geometry and adapted to SALTUS optical configuration (for radius of curvature) and (ii) a scaling of the boom to the deployment length to meet the SALTUS M1 f-number, as well as spacecraft accommodation for inflatant lines associated with the ICS (see Sec. 5) and specific actuator step size implementation for boom alignment. These are considered low-risk implementations and a standard part of the mission-unique design for the AstroMesh system.

## 3.3.3 Deployment sequence

Figure 8 illustrates the SALTUS PRM deployment sequence in six key steps. We note that each hinge will not be required to fully deploy (or fully precision latch) before a subsequent hinge actuator motion—this flexibility provides an option later for positioning optimizations, clearance optimizations, and assessment of moment of inertia impacts. The finer details of the PRM deployment sequence will be refined in phase A; this subsection presents the basic concept. Below, we outlined the six-step sequential process through full PRM deployment:



**Fig. 8** (a)–(f) SALTUS Primary Reflector Module (PRM) deployment sequence. The solar array and HGA are deployed prior to PRM deployment. The sunshield is deployed following PRM deployment. This sequence is important for avoiding a cryogenic PRM deployment (which is a more complex proposition). Note that each hinge will not be required to fully deploy or latch before the next hinge actuator in the sequence initiates its motion. This strategy allows for positioning optimizations, clearance optimizations, moment of inertia impacts, etc. and will be refined in phase A. Step 6 (f) (i–iv) shows the four actuator boom locations.

- Step 1: At launch, the SALTUS stowed truss containing the stowed M1 membrane is bound to the spacecraft at three attachment points, as shown in Fig. 8(a). At the upper and lower ends of the truss, a cable holds the assembly bundle into flexure-mounted "saddles" comprising upper and lower ridge node saddles. At the approximate center point of the bundle, a hinged "cradle," the Valley Node Cradle (VNC), restrains the truss, which is held closed with hold down and release mechanisms (HDRMs). Boom loads are shared by the root hinge and four additional tie-down points.
- Step 2: After launch ( $\sim L + 1 2$  days), ridge node cables and boom tie-down points release, thus minimizing thermal loads during subsequent maneuvers in flight to the Sun-Earth halo L2 orbit. Ridge node cables are reeled into spring-loaded mechanisms after they are cut. First motion occurs when the VNC releases. Kick-off springs on the Prime Batten propel the truss out of the VNC and rotate the truss around the boom elbow actuator, which includes an integrated ratchet to prevent bounce-back. A stepper motor actuator deploys the first boom hinge. This sequence is shown in Fig. 8(b).
- Steps 3 to 5: Subsequent boom actuators are deployed in kind sequentially until the boom is fully deployed as shown in Fig. 8(e). Each actuator deployment is choreographed to ensure that there is minimal risk of interference with other spacecraft structures and to minimize disturbances to the spacecraft. This is typically a very slow and gentle process taking hours to days depending on the number of steps and verification pauses required, as well as the precision of the actuators.
- Step 6: After the boom completes deployment steps 1 to 5, the truss deployment begins, starting with *Secondary Release*, as depicted by a real AstroMesh picture in Fig. 7(b). This is the severing of a restraint cord about the center of the stowed M1 bundle allowing the M1 bundle to bloom. *Bloom* is the event coincident with and immediately following the

Secondary Release as the truss expands rapidly and radially from the Prime Batten. This process is driven by strain energy in the stowed truss. After the dynamics of the *Bloom* have subsided, the truss deployment motors are activated and motorized deployment begins [Fig. 7(c)]. Dual redundant spoolers at the Prime Batten withdraw cable from either end of the single deployment cable that is routed through the truss diagonals. Both ends of the cable are pulled through cable tension sensing mechanisms for assessing progress and ultimately to provide the information required to terminate the deployment. As the cable is wound onto the spools, the diagonals become shorter, eventually latching into their final positions as the bays transition from partially deployed parallelograms to fully deployed rectangles. Figure 7(d) shows a real laboratory demonstration of the truss fully deployed, and Fig. 8(f) illustrates the fully deployed PRM with respect to the spacecraft, which ends the deployment sequence. At this point, finer alignment and M1 positional adjustments with respect to the CCM begin.

Note that, during deployment, the retention clips manage the PRM soft goods, which include the front and rear nets as well as the uninflated M1 membrane. These are released regularly and passively throughout the deployment. Once deployed and latched, the spoolers are backed off slightly to reduce cable tension, and the truss deployment is completed.

## 3.4 Observatory End-to-End Pointing Alignment and Stability

Northrop Grumman conducted several studies that assessed the stability provided by the ACS design, as well as the stability of the bus structure, CIM, and PRM. In addition to addressing the SALTUS ACS system performance to meet mission requirements in pointing knowledge, accuracy, and stability (Table 7), which specifically addresses capabilities at the plane of the instrument deck, we must also consider observatory end-to-end pointing alignment and stability ultimately guided by the SALTUS alignment tolerancing process. This describes the maximum allowable magnitude of perturbation as a function of rigid body motion DoF to meet the SALTUS optical performance requirements. We refer the reader to Ref. 8 for the SALTUS reflector and CCM designs, including the alignment tolerancing process and optical error budget. In this paper, we will address the mating of the spacecraft ACS performance, including vibration and jitter, with the positional in-design accuracies of the AstroMesh boom, and the observatory settling time after a maneuver.

To capture this trade at the observatory level, it is useful to think about the hierarchy as follows: (i) spacecraft level (ACS, including pointing performance and vibration/jitter), (ii) PRM level (root hinge, boom, M1/truss), and (iii) CCM level (optical elements M2...M7, described below). The spacecraft provides attitude performance measured from the instrument deck under some vibrational load, and the PRM provides alignment with respect to the CCM measured from a combination of (i) the performance from the root hinge on the instrument deck and (ii) the positioning accuracy and linear/rotational step size of the boom actuators. The superposition of these performances defines the position of the M1 boresight with respect to the M2 optic in the CCM and how long it takes the observatory to settle after a maneuver. Later in Sec. 5, we justify why the settling time is not a driving requirement for observing efficiencies. We note that, as anticipated, the tolerance ranges for M1 and M2 are tighter compared with other optics in the path, indicating their higher sensitivity in the system. Therefore, the requirement of the spacecraft attitude performance coupled with the boom actuator performance of the PRM is to reside inside the tolerance range of M1 after the settling time. M1 then passes the beam through six additional CCM optics, including an asphere (M2), a low-order deformable mirror (M3), a folding mirror (M4), a second asphere (M5), a flat field scanner/3-DoF compensator (M6), and a fast-steering mirror (M7), thus closing the end-to-end pointing alignment and stability at the observatory level. This goal is met when the optical system achieves diffractionlimited performance at 30  $\mu$ m (lambda) with margin, thus delivering >0.8 Strehl ratio.<sup>8</sup>

## 3.4.1 Structural vibration analysis

The SALTUS-induced vibration analysis leverages prior high-fidelity models of the spacecraft bus. This model was coupled with a low-fidelity model of the Payload. The Payload was modeled

Mode #	Frequency (Hz)	Description
1	0.19	M1 $\theta x$ rotation relative to spacecraft
2	0.29	M1 $\theta y$ rotation relative to spacecraft
3	0.51	M1 $\theta z$ rotation relative to spacecraft
4	0.91	M1 $x$ translation relative to spacecraft and slosh
5	0.91	M1 y translation relative to spacecraft and slosh
6	1.11	M1 z translation relative to spacecraft and slosh
7	1.11	Propellant slosh
8	3.13	Solar array primary bending
9	8.37	Solar array secondary bending
10	18.24	Solar array rotational mode
15	31.17	First spacecraft bus structural mode

Table 9 SALTUS observatory deployed structural mode estimates	Table 9	SALTUS observator	v deployed s	structural mode	estimates.
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The coupling of the low-frequency first mode of the deployed sunshield layer with the low mass of each layer is not anticipated to have substantial effects on the pointing performance. However, this will be included in a more detailed pointing vibration analysis in phase A.

with lumped masses to mimic M1, the truss, and boom (the M1-lumped mass) and the CCM (the CCM lumped mass), as well as springs at the connections to the instrument deck to mimic their estimated first structural modes, as shown in Table 9. In total, the finite element model (FEM) used for this effort has > 9 million nodes and elements. This analysis does not include deployed SM dynamics—we anticipate that the low mass of each SM layer (Table 10) coupled with the low-frequency first structural mode of the deployed layer will have negligible effects on pointing performance. However, the dynamics of each layer will be included in future analyses once the end-to-end observatory architecture is further refined. This assumption will therefore be revisited in phase A.

Northrop Grumman's induced vibration analysis technique has been used on multiple programs including ICESat-2, Landsat-8/-9, and JPSS-2. This method utilizes high-fidelity RWA models supplied by the vendor that have been correlated to test data. Both structural modes of the model, as well as the disturbance tones including primary wheel imbalance tones and bearing disturbances, have been correlated. Bearing disturbances have been modeled up to 63 times the RWA wheel speed to ensure that any low wheel speed excitations are correctly captured.

Component	Qty	CBE unit mass (kg)	Contgy. (%)	MEV (kg)
Sunshield layer 1	1	18.3	25%	22.9
Sunshield layer 2	1	19.6	25%	24.5
Hub hardware	2	1.5	25%	3.8
Booms	8	2.8	25%	28.0
Boom deployer hardware	2	20.0	25%	50.0
Central cylinder	1	8.0	25%	10.0
Misc	1	5.0	25%	6.3
Total			25%	145.4

Table 10 SALTUS sunshield module component masses.

The total MEV mass is captured under "Payload" (Table 3).

This model also includes the appropriate rotor gyroscopic coupling as well as a uniform structural damping value for all structural modes at 0.25%. The modeling technique accurately captures the disturbances as an internal force between the bearings and the RWA housing.

The induced vibration analysis considered two configurations: (1) RWAs "hard-mounted" to the bus and (2) RWAs isolated via a passive mechanical isolation system that leverages high TRL systems (e.g., Chandra and JWST). For the induced vibration analysis, the RWAs are spun up at the same wheel speed in 20 RPM increments up to 4000 RPM, providing a conservative estimate with all of the energy concentrated at the same tones. Note that the maximum allowable wheel speed (outside of safe mode) for SALTUS is 3000 RPM, which provides a 50% margin. The frequency range of interest for this analysis was from 0.01 to 500 Hz. Both translational and rotational displacements were reported at the M1-lumped mass node. The response at the M1 lumped mass node was multiplied by a model uncertainty factor (MUF) to account for model uncertainty and program maturity. The selected MUF is consistent with the concept development phase, and the amplitudes will be reduced as the design matures. The residual sum of squares for the scaled three DoF for translations or rotations was calculated to provide a total translational or rotational motion performance of the system. These performance curves were then used to calculate the RMS by finding the area under the curve and reporting 1  $\sigma$  values. We show these results in Fig. 9.

Finally, we note that the influence of the induced vibration from the cryocooler was not included in the initial system-level analysis. This omission was justified on the basis that the cryocooler disturbance frequencies are held constant throughout its operation and are above the ACS controller bandwidth. Active compensation within the CCM also mitigates any influences from the cryocooler in the optical path. In addition, the low first fundamental frequency of the PRM's boom will act as a mechanical low-pass filter for cryocooler and RWA disturbances, further minimizing the impact on M1 motion. A detailed system-level assessment that includes the cryocooler disturbances is planned for phase A. Adjustments and tuning of the structure stiffness may be implemented at that time to ensure that no interaction between known cryocooler tones and key structural modes occurs, thus maintaining positive margins.

#### **3.4.2** PRM settling time after maneuvering

A conservative bang-bang slew was performed to estimate the initial M1 pointing error from a maneuver. The max torque from one RWA is applied about the spacecraft X axis for 50 s; then it is applied in the opposite direction to bring the observatory to rest. This maneuver results in an  $\sim 6$  deg slew about the X axis. Once the body is at rest, the motion of M1 is reported, resulting in an initial displacement of 0.00015 radians. From this initial displacement, various structural damping values were assumed, and using the log decrement method, the displacement is propagated forward in time. As seen in Fig. 10, the M1 rotational displacement as a function of time

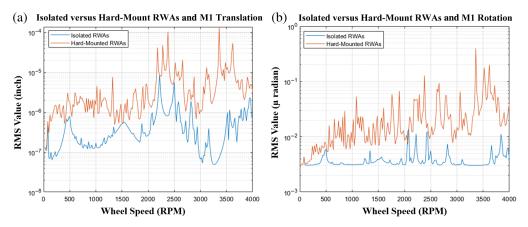


Fig. 9 (a) SALTUS observatory isolated versus hard-mounted RWAs induced vibration RMS (1  $\sigma$ ) translational displacements of M1. (b) SALTUS observatory isolated versus hard-mounted RWAs induced vibration RMS (1  $\sigma$ ) rotational displacements of M1.

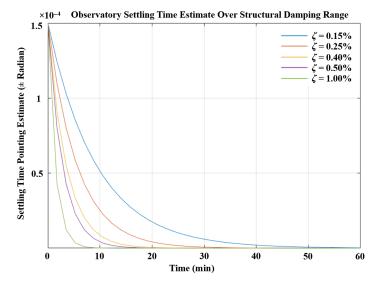


Fig. 10 Rotational displacement of M1 as a function of time for a range of structural damping values.

can be seen for various given structural damping values. For bare metallic or composite structures, a value of 0.15% to 0.25% is typically used, and this range is captured in Fig. 10. However, this is highly conservative and does not include the benefits of other components such as thermal blanketing and harnessing, which all contribute to additional damping. Further, we have an onorbit point of reference for a large deployable structure from SMAP and its 6-m RBA (Table 8). This included a large boom with two locked-out hinges, similar to the SALTUS design. The first two primary mode values were measured at 0.5% and 0.7%, respectively.

As noted above, we assumed a very conservative approach for the values and assumptions in settling time estimates. Additional methods can be employed to further mitigate settling time and pointing errors and will be investigated later in the program. These include leveraging a slew profile that smooths the transitions to limit the system jerk, a fly-cast maneuver in which the ACS system actively removes energy from the system by counteracting excitation, and other structural methods to introduce damping (such as damping tape or tuned mass dampers). We discuss settling time as it pertains to on-sky efficiency in Sec. 5.2.1.

In the PRM design, we also considered M1's stability with respect to M2 and found this to be primarily translation-driven by tip/tilt mechanisms in the boom and the wrist hinge—see Fig. 8(f). This stability was assessed via the FEM of the deployed PRM, assuming a 15-m truss diameter (to hold the 14-m M1), three boom sections, and four single-axis actuators. Each boom section and hinge actuator was measured separately and then combined analytically. Note that the analysis captures at minimum one axis of rotation at each of the four hinge locations that are typically not parallel to any other axis of rotation. These locations are the root hinge between the boom and spacecraft, two intermediate hinges on the boom, and the wrist hinge between the reflector and boom. These are labeled in Fig. 8(f) as (i)–(iv). For a total boom length of ~17 m, the system is required to produce an M1 tip/tilt step size of 2.42  $\mu$ rad (0.0001389 deg) and a linear step size of 0.025 mm. Table 8 shows previously demonstrated Northrop Grumman missions on orbit with a similar performance, and the SALTUS phase A design will refine this trade.

## 3.4.3 ACS performance

The SALTUS ACS pointing knowledge, accuracy, and stability provides 1.19 arcsec  $(1 \sigma)$ , 1.20 arcsec  $(1 \sigma)$ , and 0.66 arcsec  $(1 \sigma)$  at the root hinge, respectively, demonstrating a significant margin to meet spacecraft requirements (180%, 736%, and 189%; see Table 7). Once a science target is acquired, the observatory offers <0.5 arcsec pointing stability over a 20-s period in between CCM fast-steering mirror (M7) adjustments. With this performance, the ACS enables M1 to capture the requested SALTUS science target and propagate it to M2 in the CCM.

# 4 Sunshield Design

#### 4.1 Concept Overview

The SALTUS baseline SM comprises two thin-film layers separated by  $\sim 2$  m in the deployed configuration. This separation is driven by radiative cooling considerations to attain an M1 temperature of <45 K, which is maintained throughout the mission lifetime. Each layer is deployed, tensioned, and structurally supported by a deployable mast system. The two sunshield layers, underlying structures, and associated deployment mechanisms are assembled onto a central composite cylinder, which sits outside the CIM, allowing the SM subsystem to be fully flight acceptance tested by NeXolve and Redwire Space and delivered to Northrop Grumman for integration into the spacecraft with low complexity. Northrop Grumman designed CIM attachment points (discussed in Sec. 3.2.2) for compatibility with the SM integration. The SM structure also provides a stiff and stable root boundary condition for sunshield layers and serves as the primary structural load path for the system during launch.

The SM design heavily leverages several solar sail designs spearheaded by NeXolve and Redwire Space. Most recently, the Solar Cruiser<sup>12,13</sup> solar sail development program has matured a 40 m<sup>2</sup> aperture to TRL-8 through full flight qualification testing. The deployable masts for Solar Cruiser are 30 m long, comparable in length to the mast design for SALTUS. These masts, discussed in more detail in Sec. 4.3.1, have been designed and analyzed to accommodate the structural loading anticipated for SALTUS. A full mast test campaign has resulted in structural performance verification and correlated models. In this section, we discuss heritage and TRL; the SM structure, including stowed and deployed configurations; and the deployment sequence. Finally, we expand on key design considerations unique to SALTUS that drove design decisions such as the sunshield area, shape, and positioning with respect to M1.

#### 4.2 Heritage and TRL

The two-layer SALTUS sunshield draws a strong heritage from NeXolve's experience in designing and building gossamer membrane systems such as the JWST sunshield, the solar sails on missions such as NEAScout and Solar Cruiser, and deorbiting and dragsail devices as deployed on Nanosail-D. We included six exemplar developments and deployments in Table 11, which includes comprehensive detail of the system features, surface (material) features, and packaging and deployment designs. In the right-most column of Table 11, we show the current SALTUS baseline as it relates to other programs, most notably the Solar Cruiser mission currently in successful operation with significant crossover in design with SALTUS. Indeed, the selected materials are based primarily on thermal performance coupled with mechanical considerations, and the design would likely use Kapton (JWST) or CP1 (Solar Cruiser) for the film material, with optical coatings comprised of vapor-deposited aluminum (VDA, typically 1000 Å) and highemissivity coatings (Si) on the back side for increased heat rejection. These material and coating choices will be down-selected pending a full system end-to-end thermal analysis in phase A. The SALTUS design therefore takes advantage of tried and tested materials and processes developed for successful programs, resulting in a low-risk approach while meeting thermal and mechanical requirements. Key parameters included in Table 11 are discussed in Sec. 4.3.1.

#### 4.3 Sunshield Module Structure and Deployment Sequence

## 4.3.1 Structure

Figure 11 shows the typical features and layout that will be employed for SM layers. Roll widths vary depending on the material selected (ranging from 36 to 60 in.) and will drive the number of seams required to span the 20-m sunshield width. Seams will be parallel to the long edge with Z-folding perpendicular to these seams as the sunshield layer membranes are manufactured. Seaming processes are dependent on the material selected; some options include solvent bonding (CP1), thermal spot bonding (Kapton), or the use of silicone adhesives (e.g., Nusil). Seams typically have grounding "jumpers" installed to ensure that the sunshield membrane is electrically continuous and can dissipate any charge that may build up through a ground connection with the spacecraft.

Parameter	S4	Nano sail-D	JWST SMA	JWST MCA	NEAScout	Solar Cruiser	SALTUS
Summary system features							
Architecture	4-quad	4-quad	5-layer	4 covers	Monolithic	4-quad	Monolithic
Years active (*delivered)	2005-	2008 to 2011	2016*	2016*	2019	2019 to 2026	I
Quads/layers	4	4	£	-	÷	4	Ŋ
Quad/layer shape	Right triangle	Right triangle	6 sided	Rectangular	Rhombus	Right triangle	Rectangular
Deployed surface shape	Flat	Flat	Doubly curved	Singly curved	Flat	Flat	Flat
Total surface area	400 m <sup>2</sup>	$10 \text{ m}^2$	145 to 166 m <sup>2</sup>	>20 m <sup>2</sup> each	86 m <sup>2</sup>	1653 m <sup>2</sup>	$\sim 2000 \text{ m}^2$ (1)
Quad/layer surface area	100 m <sup>2</sup>	2.5 m <sup>2</sup>	145 to 166 m <sup>2</sup>	>20 m <sup>2</sup> each	86 m <sup>2</sup>	$\sim$ 413 m <sup>2</sup>	$\sim 1000 \text{ m}^2$ (1)
Film material	CP1	CP1	Kapton	Kapton	CP1	CP1	CP1
Material thickness	2.5 μm	2.5 μm	1 mil, 2 mil	1 mil	2.5 µm	2.5 μm	12.7 µm
System surface features							
Coating	1000 Å VDA	1000 Å VDA	VDA or Si	VDA or Si	1000 Å VDA	1000 Å VDA	1000 Å VDA
Ripstop	Encap thread	Encap thread	TSB	TSB	TCP1	TCP1	TCP1
Electrical Jumpers	I	Yes	Yes	Yes	Yes	Yes	Yes
Edge reinforcement	I	Yes	Yes	Yes	Yes	Yes	Yes
Corner reinforcement	Yes	Yes	Yes	Yes	Yes	Yes	Yes
Install method	Adhesive bond	Tape	2-part adhesive	TSB	PSA, resin bond	PSA, resin bond	PSA, resin bond
Seam and Ripstop install.	Thermal	Thermal	TSB	TSB	Resin bond	Resin bond	Resin bond
System packaging and deployment	yment						
Folded/stowed/packaged	Z-fold, rolled to four spools	Z-fold, rolled to one spool	Z-fold and stacked	Flat	Z-fold, rolled to one spool	Z-fold, nested, roll to one spool	Each Z-folded, wrapped in two spools
Packaged restraints/tearaways	None	Bumper	MRDs	MRDs	Restraint, tearaways	Restraint, tearaways	Restraint, tearaways
Deployment approach	Pull out via booms	Pull out via booms	Complex	Rel. mech., rolled	Pull out via booms	Pull out via booms	Pull out via booms
Tensioned method	3-corner pull via ATK boom	3-corner pull via metallic TRAC boom	6-point corner pull	I	4-corner pull via metallic TRAC boom	3-corner pull via composite TRAC boom	4-corner pull via composite TRAC boom
The table contains heritage tensioned-membrane systems developed by NeXolve and Redwire Space. Note that the SALTUS material thickness is driven by micrometeoroid considerations. The Solar Cruiser development is the most recent flight heritage example. (1) Layer 2 area of ~1000 m <sup>2</sup> from ~50 m × ~20 m dimension. Layer 1 area estimated at ~931 m <sup>2</sup> from ~48.5 m × ~19.2 m.	sioned-membrane sys e most recent flight he	stems developed by Ne sritage example. (1) Lay	Xolve and Redwire S /er 2 area of ∼1000 r	Space. Note that the $n^2$ from ~50 m × ~2	SALTUS material thick 0 m dimension. Layer 1	mess is driven by micrometeo area estimated at ${\sim}931~{\rm m}^2~{\rm fr}$	proid considerations. The rom $\sim$ 48.5 m $\times$ $\sim$ 19.2 m.

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 Table 11
 SALTUS sunshield module heritage.

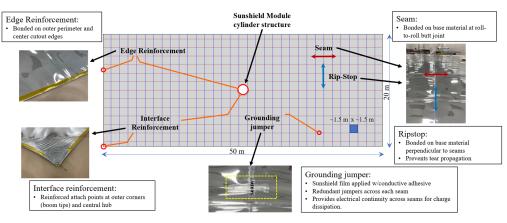
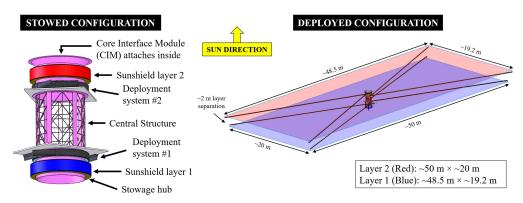


Fig. 11 SALTUS sunshield layer features and layout.

Perpendicular to the seams are ripstops, typically spaced to create a square grid pattern with the seams. Ripstops are to limit the propagation of a tear should one occur. The installation of ripstops is similar to seams. Trimmed edges, found at the outer perimeter and at the circular cutout where the SM's cylindrical structure resides (red circle in the center of Fig. 11, and labeled as "Central Structure" in the stowed configuration in Fig. 12), are reinforced to prevent tears and to distribute tensioning load across the sunshield membrane. Constructions vary from using Kapton tape (with a cover overlay to mitigate adhesive leach out) to bonding on strips of the base material to "double up" the thickness at this edge. Corners have additional reinforcements where the grommet attachment point is located, typically a stack-up of stainless steel (3 to 5 mil depending on membrane tensioning loads) and additional covers for optical purposes and grounding features. Connection to the mast can be through a small clevis/pin attached to the grommet for ease of installation/removal to the cable/tensioning system at each of the boom tips. Grounding of the membrane to the spacecraft can be done here or at the CIM interface if attached (or both).

Triangular Rollable and Collapsible (TRAC) masts are constructed from two thin gauge high-strain composite (HSC) tape springs that are bonded along one edge to form a triangular cross-section. This geometry can be flattened and then rolled onto a hub for stowage (see Fig. 12). Thirty-meter TRAC masts, the same length required for the SALTUS sunshield, have been demonstrated and matured to TRL-6 as part of the Solar Cruiser solar sail system. The TRAC mast provides very high bending stiffness for a given flattened height. In other words, the mast provides excellent performance for a minimized system mass and stowage volume. Other rollable cross-sectional geometries, such as the Collapsible Tubular Mast (CTM), could also be considered for the masts. Although the CTM cross-section provides substantially higher



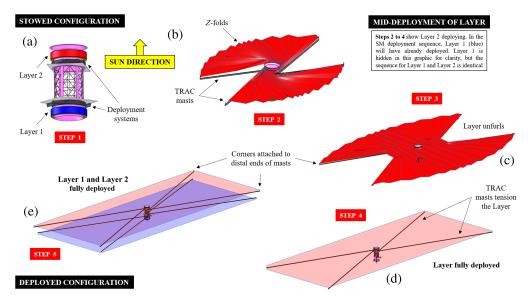
**Fig. 12** SALTUS sunshield stowed and deployed configurations. The stowed configuration shows a zoomed-in image of the sunshield module (SM), which sits outside and attaches to the CIM. The smaller ~48.5 m × ~19.5 m layer 1 deploys first, followed by the larger 50 m × ~20 m layer 2, which prevents a cryogenic deployment of the second layer in the deployment sequence. Layer 2 will be the last major deployment of the SALTUS observatory.

torsional stiffness and stability than the TRAC variant, further development work would be needed to fabricate and demonstrate the CTM at the required length and stiffness needed for SALTUS. However, the CTM technology is being matured as part of NASA Langley's ACS3 mission and could certainly be a viable option for SALTUS, given the timeframe for the mission. Apart from cross-sectional geometry, these two mast technologies are very similar with respect to the composite materials used, as well as their spooling and deployment behavior, and are therefore considered interchangeable within the sunshield subsystem. The composite TRAC masts are manufactured from carbon fiber-reinforced polymer (CFRP) composite materials. The high-modulus carbon fibers are predominantly oriented in the longitudinal axis, providing optimized compression and bending stiffness at a minimized mass. Furthermore, the composite laminate architecture is optimized for near-zero CTE to ensure on-orbit shape stability. The SALTUS SM team has extensive experience with composite mast design, and further optimizations can be considered if necessary.

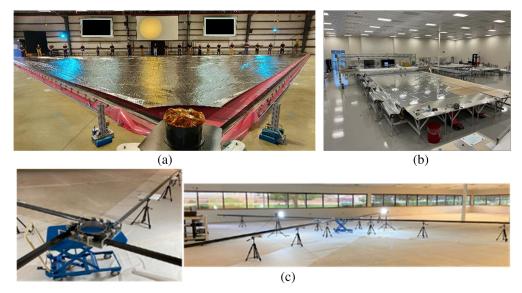
## 4.3.2 Deployment sequence

The sunshield is the last major deployment for the observatory; it follows solar array and HGA deployments and PRM deployment. Sunshield layer 1 (the smaller layer closer to the PRM) is deployed first, thus ensuring that no preceding subsystem/component deployment is a cryogenic deployment, which would require additional cryogenic development and testing. Layer 2 is the final deployment in the sequence. We describe the sequence, in reference to Fig. 13, as follows:

• Steps 1 to 3: Step 1 shows the SM in a fully stowed state. The rectangular sunshield layers are pleated (i.e., *z*-folded) in the long axis and then spooled onto a cylindrical hub for stowage. Adjacent to each stowed layer is its associated deployment system, comprised of four TRAC masts that are co-spooled on a stowage hub and are used to deploy and tension each layer. Steps 2 to 3 show the mid-deployment of layer 2 following TRAC mast deployment from their stowage hubs. As noted in the figure, layer 1 will deploy first and has been hidden for clarity, but the sequence is identical. Layers can be deployed separately via independent deployment systems (a single brushless DC (BLDC) motor), which occurs



**Fig. 13** SALTUS sunshield deployment sequence. (a) Stowed configuration showing each sunshield layer and deployment system location. The stowed layers, deployment system, and TRAC masts are co-spooled on a stowage hub. (b) TRAC masts are deployed using a single brushless DC motor mechanism. (c) The deployment mechanism continues to unfurl the layer. (d) Tension is driven into the layer on full deployment. The corners of each layer are mechanically attached to the distal ends of each mast. (e) Steps 1 to 4 are repeated for the second layer, ensuring a non-cryogenic deployment for both layers. Once both layers are deployed, all major observatory deployments are complete, and the cryogenic thermal environment begins to stabilize to < 45 K.



**Fig. 14** (a) Single-deployed quadrant of the Solar Cruiser sail system utilizing 30 m TRAC masts with a side dimension of 40 m. (b) Membrane manufacturing facility at NeXolve, which is capable of producing sunshield layers to meet the SALTUS required area. (c) A four-mast TRAC deployment system that has been matured to TRL-6.

in <60 min and utilizes <20 W of power. These single-motorized mechanisms contain a variety of features to stabilize the system for launch, control boom deployment in-flight, and to provide the necessary root boundary constraints for deployed structural performance. The corners of the stowed rectangular layer are mechanically attached to the distal ends of the masts. Figure 14(c) illustrates a four-mast TRL-6 deployment.

• Steps 4 to 5: Once the masts are deployed, the bearing-mounted sunshield layer is fully unfurled. Tension is driven into each layer upon full deployment, resulting in a planar layer that meets key performance parameters for flatness and deployed first mode natural frequency. Once step 4 is completed for layer 1, steps 1 to 4 are repeated for layer 2, resulting in the full two-layer sunshield deployment, as shown in step 5.

The deployment mechanism that we selected for SALTUS will heavily leverage the Sail Deployment Mechanism (SDM) designed for the Solar Cruiser solar sail.<sup>12,13</sup> The Solar Cruiser SDM was designed to deploy four 30-m long TRAC booms in a square configuration and has been matured to TRL-6 as part of the Solar Cruiser solar sail flight qualification campaign.

## 4.4 Key SALTUS Design Considerations

The initial sizing of the sunshield was driven by the maximum achievable FOR of the SALTUS observatory using current state-of-the-art capabilities in designing and manufacturing tensioned-membrane architectures. As previously noted, the SALTUS sunshield heavily leverages the recent Solar Cruiser solar sail development program, which has brought a 40 m  $\times$  40 m deployable membrane to TRL-6, involving a full environmental test campaign. A full-scale quadrant of the Solar Cruiser solar sail is shown in Fig. 14(a).

Due to SALTUS CONOPs, the sunshield transverse dimension can be much smaller than the longitudinal dimension, which is advantageous to the system mass. A 20-m transverse dimension, which is the maximum membrane dimension that can be manufactured using existing ground support equipment (GSE) and facilities at NeXolve, was therefore selected. The resulting rectangular architecture represents a slight departure from Solar Cruiser's square architecture; however, the masts and membranes used in Solar Cruiser are similar in size to what is envisioned for SALTUS and therefore do not present scaling challenges. The most substantial modification will involve adjusting mast angles within the deployment mechanism to achieve the rectangular geometry. Importantly, the SALTUS design does not involve lengthening the masts beyond 30-m (demonstrated for Solar Cruiser) or widening the membrane beyond 20-m, which means that existing GSE and processes can be utilized, as shown in Fig. 14(b).

Given that the SALTUS SM design is based on Solar Cruiser's deployment sequence, there are no membrane cable management features similar to JWST. As noted above, the membrane is tensioned via TRAC masts that are deployed by motors in the stowage hub. Some short cables are present, however, to attach the membrane to the constant force tensioning device at the distal end of the masts, as highlighted in Figs. 13(c) and 13(e). However, because the membrane storage and deployment concept involve storing the SM layers tightly spooled in the CIM for launch, the need for complex membrane launch restraints and management features is eliminated. In addition, the SM deployment occurs simultaneously with the TRAC masts, also eliminating the need for tensioning cables and corresponding cable management. Finally, our design also considers how critical the membrane shape and edge alignment are, to ensure the < 45 K cryogenic environment. Edge alignment is important for SALTUS, but less critical than JWST, due to over-sizing the total footprint. This design feature guarantees that layer 2, the hotter layer, will never be in view of the Payload. The SALTUS concept derived from solar sails is thus significantly less complex than the JWST sunshield.

As the SALTUS mission concept is refined in phase A, detailed modeling and analysis of the sunshield system, both structural and thermal, may lead to additional design trades. As an example, the performance of the telescope may greatly benefit from the addition of one or more membrane layers, aiding in the protection against MMs. In addition, alternative optical coatings having improved emissivity and thermal rejection capabilities may be investigated. Deployment thermal analysis will also be considered; however, we note that membrane and deployment mechanisms and other SALTUS SM hardware have JWST legacy and have been qualified over a wide range of operating temperatures that envelope the expected SALTUS flight conditions.

# 5 Lifetime: A Two-Consumable Architecture

## 5.1 Propellant System

#### 5.1.1 Overview

The SALTUS propellant tank has been sized to carry a total hydrazine propellant mass of 1093.7 kg MEV. Approximately 40% of this budget is required to reach the SALTUS orbit via impulsive burn and *X/Y* attitude control maneuvers, corresponding to the  $\Delta V$  budget in Table 2. The remaining ~60% is required for RWA MUs (~40%) and station keeping (~20%). Our calculations show that MU is dominated by SRP and inertia, both unique to SALTUS, and thus, we consider MU maneuvers to be the dominant propulsion mode that limits the mission lifetime when considering the "propellant consumable" in the two-consumable architecture (the other consumable being ICS, discussed in Sec. 5.2). SRP accumulates across the SALTUS FOR over the mission lifetime (including CG migration), which scales directly from the total sunshield larger layer area of ~1000 m<sup>2</sup>. In addition, as shown in the table in Fig. 5(b), the observatory produces very large inertial moments (>80,000 km  $\cdot$  m<sup>2</sup> in a deployed configuration at BOL), thus requiring large RWAs to meet an acceptable slewing performance across the FOR. These factors require significantly more propellant mass for MUs than other conventional space missions and ultimately define the lifetime.

We consider MU calculations to be a bounding case because the analysis does not capture strategies that minimize momentum accumulation, e.g., strategic observation planning for efficient target selection, which could extend the mission lifetime even further. Currently, the propellant subsystem provides a positive margin at the 5-year mission baseline with a tank capacity of 50.1% (Table 7). In this subsection, we expand on SALTUS on-sky efficiency and MU and discuss migration of the static margin (i.e., the distance between CG and center of pressure, CP) from BOL to EOL.

#### 5.1.2 Operational on-sky efficiency

The operational efficiency,  $\eta$ , of SALTUS for the GTO program is the ratio of time observing to the total time (also characterized as one minus the fraction of time spent not observing), given as

$$\eta = \frac{\text{time observing}}{\text{all time}} = \frac{(\text{all time}) - (\text{time not observing})}{\text{all time}}.$$
 (1)

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This  $\eta$  requirement for SALTUS is 60%. Although the GO observing program is currently unknown, the GTO's performance discussed herein is directly applicable to the GO program. SALTUS will not observe during slew and/or settling time, MUs, ground contacts, or observatory safe modes. We carried out a parametric assessment assuming a slew, MU, and settle before and after an observation, which shows that the determination of observational efficiency,  $\eta$ , can be reduced to a single parameter—allowable settle time,  $\sigma$ . Note that, per Table 5, the worst-case power mode does in fact assume an observation during ground contacts for conservatism in power sizing, and although the observatory does have the ability to accommodate this mode, it should not affect the outcome of  $\eta$  or  $\sigma$ . The (time not observing) variable in Eq. (1) can be broken up into the following components: the observatory overhead,  $\gamma$ ; the percentage of time lost to communications,  $n(S + \sigma + L_T)/7.24$ ; the percentage of time lost to MU,  $((24/\delta).t_d)/24$ ; and the percentage of time lost to spacecraft safe mode from flight actuals,  $W_{sc} = M/365$ , where M is the total time the spacecraft spends in safe hold mode over 1 year. Equation (1) now becomes

$$\eta = \frac{24 - \left(\frac{24}{L} \cdot (S + \sigma)\right)}{24} - \gamma \left( \left(\frac{n(S + \sigma + L_T)}{7.24}\right) + \left(\frac{\frac{24}{\delta} \cdot t_d}{24}\right) + W_{\rm sc} \right),\tag{2}$$

where L is the length of observation, S is the slew time,  $\sigma$  is the allowable settle time and is a variable to be solved for in this derivation, n is the number of communications contacts per week,  $L_T$  is the total link time,  $\delta$  is the MU interval, and  $t_d$  is the time taken to unload the RWAs. Therefore,

$$\eta = 1 - \left(\frac{S+\sigma}{L}\right) - \gamma \left[ \left(\frac{n(S+\sigma+L_T)}{7.24}\right) + \left(\frac{t_d}{\delta}\right) + W_{\rm sc} \right],\tag{3}$$

$$\eta = 1 - \left(\frac{S+\sigma}{L}\right) - \left(\frac{\gamma.n(S+\sigma)}{7.24}\right) - \left(\frac{\gamma.n.L_T}{24}\right) - \left(\frac{\gamma.t_d}{\delta}\right) + \gamma.W_{\rm sc},\tag{4}$$

$$-\left(\frac{\sigma}{L}\right) + \left(\frac{\gamma.n.\sigma}{7.24}\right) = 1 - \left(\frac{S}{L}\right) - \left(\frac{\gamma.n.S}{7.24}\right) - \left(\frac{\gamma.n.L_T}{24}\right) - \left(\frac{\gamma.t_d}{\delta}\right) - \gamma.W_{\rm sc} - \eta. \tag{5}$$

Solving for the allowable settle time,  $\sigma$ , we find

$$\sigma = \frac{1 - \left(\frac{S}{L}\right) + \left(\frac{\gamma.n.S}{7.24}\right) - \left(\frac{\gamma.n.L_T}{24}\right) - \left(\frac{\gamma.t_d}{\delta}\right) - \gamma.W_{sc} - \eta}{\left(\frac{1}{L}\right) + \left(\frac{\gamma.n}{7.24}\right)}.$$
(6)

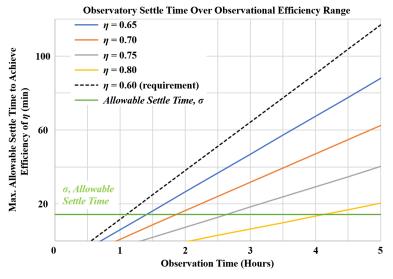
Evaluating Eq. (6) for a range of L and potential values of  $\eta$ , we use the following analysis to determine input parameters. We assume SALTUS targets are uniformly distributed over the FOR. The observatory is capable of slewing 180 deg in  $\sim$  30 min via six RWAs (see Sec. 3.2.7) at 50% max allowable wheel speeds of 3000 RPM (providing a 50% margin), and using the maximum inertia in the deployed configuration from Fig. 5(b), we find a mean slew S of ~15 min.  $L_T$  is a total of 7 h per week distributed per the science CONOP, contributing 4.2% of a day.  $\delta$  is expected to occur at the shortest interval, i.e., the worst-case attitude and at BOL when CG-CP is a maximum, which is every  $\sim 4$  h and takes  $\sim 5$  min to complete. This contributes 2.1% of the day. We combine this with a historical average for LEOStar-3 safe mode duration,  $W_{SC}$ , at 3 days per year, or 0.8% per day. If the mean observation, L, is 4 h (currently, the mean is estimated to be  $\sim 5$  h, but we use 4 h for added conservatism), there are six observations per day, thereby resulting in 5.2% of a day in slewing modes. These activities account for 12.3% of the time. We added  $\gamma = 25\%$  observatory overhead (i.e.,  $12.3\% \times \gamma$ , where  $\gamma = 1.25$ ) to capture uncertainties, thereby providing extra contingency to the design process, yielding 15.4% of time lost per day. This results in  $\eta = 84.6\%$  observational efficiency, well in excess of the  $\eta = 60\%$  requirement, as shown in Table 12.

Solving Eq. (6) with the above inputs yields an allowable settle time,  $\sigma$ , of 13 min CBE (~1% of a day), as indicated by the green horizontal line in Fig. 15, which shows the range of compliance against the  $\eta = 60\%$  efficiency requirement. We note that, to meet  $\eta = 60\%$ , <27.6% of the day must be spent settling, or 4.6% of a day per observation (~1.1 h).

Variable	% Lost per day (%)	Value
Communications contacts (1)	4.2	7 h/week
Momentum unload interval (2)	2.1	5 min/4 h
Spacecraft safe hold duration (3)	0.8	3 days/year
Slewing modes (4)	5.2	6 slews/day
Total: (1) + (2) + (3) + (4)	12.3	-
Observatory overhead (5)	3.1	25% of total
On-sky efficiency	15.4	84.6%

 Table 12
 SALTUS on-sky efficiency key and driving variables.

(1) 7 h per week distributed per CONOP. (2) Expected to occur at the shortest interval, worst case BOL attitude. (3) From LEOStar-3 flight actuals. (4) CBE observation time is 5 h; 4 h is used for added buffer. Therefore, assume six observations per day, each requiring a slew to target. (5) Observatory overhead to capture uncertainties in the design process, which we add as an additional  $\gamma = 25\%$  to 12.3%.



**Fig. 15** SALTUS maximum allowable settle time to achieve a given observing efficiency as a function of observation time. For shorter observations, the mean efficiency is greater than the science mission requirements. Given the requirement of  $\eta = 0.60$ , the mean observation time can be as short as 1 h (current mean observation time is 5 h CBE), and SALTUS will still meet this requirement.

Effectively, this means that, with  $\sigma = 13 \text{ min}$ , L can be as short as 1 h (recall, the current mean L = 5 h CBE), indicating that the SALTUS observing efficiency is highly insensitive to the settling time.

## 5.1.3 Momentum unloading, torque, and static margin

The interval between MUs is dependent on the separation of the CG to the CP, the observatory attitude, and the sunshield properties. The table in Fig. 5(b) shows observatory CG locations, in meters, in X, Y, and Z with respect to the spacecraft origin, which we define to be the geometric center of the separation ring plane located at the ~aft end of the spacecraft [labeled "Sep plane" in Fig. 5(c)]. We designed CG to approximately reside at the X- and Y-centers of the GEOStar-3 primary structure. CP is located at the geometric center of sunshield layer 2 (on the spacecraft side; the 50 m × 20 m layer) at XYZ coordinates 0 m, 0 m, + 3.88 m. By assessing the mass and the XYZ location of all major SALTUS spacecraft components, flight system components, and

Payload components, we calculated CG at launch and over the full mission lifetime (BOL-EOL). We assessed the initial CG LV dispersions and linear motion as the consumables are expended over mission life. Because we know the momentum storage capacity of the selected RWAs, we can calculate a map of MU intervals as a function of observatory pitch and roll angles, corresponding to different attitudes in the FOR.

We show this result in Fig. 16(a), where we highlighted in a purple rectangular box the MU interval in hours at BOL as a function of the SALTUS FOR, as defined by  $\pm 20$  deg of pitch and  $\pm 5$  deg of roll. By finding the minimum MU interval in the FOR, we can identify the attitude that generates maximum momentum accumulation. As shown, the worst-case MU interval is 4.71 h at BOL, which is less frequent than the observation length of 4 h used in our efficiency calculation in Sec. 5.1.2. Moreover, this worst-case MU interval increases over the mission life as the propellant and inflatant gas are consumed, and therefore, this 4-h MU interval is used to size the propellant mass over the SALTUS mission lifetime. AT EOL, the MU interval minimum is 6.59 h, as shown in Fig. 16(b). To assess the adequacy of the propellant capability of the proposed

#### (a) BOL: Momentum Unload Interval As a Function of Observatory Pitch and Roll in FOR

5.5 5 4.5	-24	-22												2				10	10				20		
5.5 5 4.5	5.87	5.67	-20	-18	-16	-14	-12 5.01	-10 4.93	4.86	-0	4 78	-2	4 75	4.75	4 77	4.80	4.84	4.90	4.97	14 5.06	16 5.16	18 5.28	20 5.43	22 5.59	24 5.77
4.5	5.85	5.66	5.49	5.34	5.21	5.09	5.00	4.92	4.86	4.81	4.77	4.75	4.74	4.74	4.76	4.79	4.84	4.89	4.97	5.06	5.16	5.28	5.42	5.58	5.77
	5.84	5.64	5.47	5.32	5.20	5.08	4.99	4.91	4.85	4.80	4.77	4.74	4.73	4.74	4.76	4.79	4.83	4.89	4.96	5.05	5.16	5.28	5.42	5.58	5.77
4	5.83	5.63	5.46	5.31	5.19	5.08	4.98	4.90	4.84	4.79	4.76	4.74	4.73	4.74	4.75	4.78	4.83	4.89	4.96	5.05	5.16	5.28	5.42	5.58	5.77
	5.81	5.62	5.45	5.31	5.18	5.07	4.98	4.90	4.84	4.79	4.75	4.73	4.73	4.73	4.75	4.78	4.83	4.89	4.96	5.05	5.16	5.28	5.42	5.59	5.77
	5.80	5.61	5.44	5.30	5.17	5.06	4.97	4.89	4.83	4.78	4.75	4.73	4.72	4.73	4.75	4.78	4.82	4.88	4.96	5.05	5.16	5.28	5.42	5.59	5.77
	5.79	5.60	5.43	5.29	5.16	5.05	4.96	4.89	4.83	4.78	4.75	4.73	4.72	4.73	4.74	4.78	4.82	4.88	4.96	5.05	5.16	5.28	5.42	5.59	5.78
	5.78 5.77	5.59 5.58	5.43 5.42	5.28	5.16	5.05	4.96 4.95	4.88	4.82	4.77	4.74	4.72	4.72	4.72	4.74	4.78	4.82	4.88	4.96	5.05	5.16 5.16	5.28 5.28	5.43 5.43	5.59 5.60	5.78 5.78
	5.76	5.58	5.42	5.27	5.15	5.04	4.95	4.87	4.81	4.77	4.74	4.72	4.71	4.72	4.74	4.77	4.82	4.88	4.96	5.05	5.16	5.28	5.43	5.60	5.78
	5.75	5.57	5.40	5.26	5.14	5.03	4.94	4.87	4.81	4.77	4.73	4.72	4.71	4.72	4.74	4.77	4.82	4.88	4.96	5.05	5.16	5.29	5.44	5.60	5.80
	5.75	5.56	5.40	5.26	5.13	5.03	4.94	4.87	4.81	4.76	4.73	4.72	4.71	4.72	4.74	4.78	4.82	4.89	4.96	5.06	5.17	5.29	5.44	5.61	5.80
0	5.74	5.55	5.39	5.25	5.13	5.03	4.94	4.86	4.81	4.76	4.73	4.71	4.71	4.72	4.74	4.78	4.83	4.89	4.97	5.06	5.17	5.30	5.45	5.62	5.81
	5.73	5.55	5.39	5.25	5.13	5.02	4.94	4.86	4.81	4.76	4.73	4.71	4.71	4.72	4.74	4.78	4.83	4.89	4.97	5.06	5.17	5.30	5.45	5.62	5.82
	5.73	5.54	5.38	5.24	5.12	5.02	4.93	4.86	4.80	4.76	4.73	4.72	4.71	4.72	4.74	4.78	4.83	4.89	4.97	5.07	5.18	5.31	5.46	5.63	5.82
	5.72	5.54	5.38	5.24	5.12	5.02	4.93	4.86	4.80	4.76	4.73	4.72	4.71	4.72	4.75	4.78	4.83	4.90	4.98	5.07	5.19	5.32	5.47	5.64	5.83
	5.72 5.71	5.54 5.53	5.38 5.38	5.24 5.24	5.12 5.12	5.02 5.02	4.93 4.93	4.86 4.86	4.80	4.70	4.73	4.72	4.72	4.73 4.73	4.75	4.79	4.84	4.90	4.98	5.08 5.08	5.19 5.20	5.32 5.33	5.47 5.48	5.65 5.66	5.84 5.85
	5.71	5.53	5.37	5.24	5.12	5.02	4.93	4.86	4.81	4.77	4.74	4.72	4.72	4.73	4.76	4.79	4.85	4.91	4.99	5.08	5.20	5.34	5.49	5.67	5.87
	5.71	5.53	5.37	5.24	5.12	5.02	4.93	4.86	4.81	4.77	4.74	4.73	4.72	4.74	4.76	4.80	4.85	4.92	5.00	5.10	5.21	5.35	5.50	5.68	5.88
	5.71	5.53	5.37	5.24	5.12	5.02	4.94	4.87	4.81	4.77	4.74	4.73	4.73	4.74	4.77	4.81	4.86	4.93	5.01	5.11	5.22	5.36	5.51	5.69	5.89
-4.5	5.71	5.53	5.37	5.24	5.12	5.02	4.94	4.87	4.81	4.77	4.75	4.73	4.73	4.75	4.77	4.81	4.86	4.93	5.02	5.11	5.23	5.37	5.52	5.70	5.90
	5.71	5.53	5.37	5.24	5.12	5.02	4.94	4.87	4.82	4.78	4.75	4.74	4.74	4.75	4.78	4.82	4.87	4.94	5.02	5.12	5.24	5.38	5.53	5.71	5.92
	5.71	5.53	5.38	5.24	5.13	5.03	4.94	4.88	4.82	4.78	4.76	4.74	4.74	4.76	4.78	4.83	4.88	4.95	5.03	5.13	5.25	5.39	5.55	5.73	5.93
-6	5.71 -24	5.53 -22	5.38 -20	5.24 -18	5.13 -16	5.03 -14	4.95 -12	4.88	4.83	4.79	4.76	4.75	4.75	4.76	4.79	4.83	4.89	4.96 10	5.04 12	5.14 14	5.26 16	5.40 18	5.56 20	5.74	5.95 24
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	EO	DL:	Mo	mer	ntur	n Ui	nload	l In	terv	val A	As a	Fu	ncti	on o	f Oł	oser	vat	ory	Pite	ch a	nd ]	Roll	l in 1	FO	R
	-24	-22	-20	-18	-16	-14	-12	-10	-8	-6	-4	-2	0	2	4	6	8	10	12	14	16	18	20	22	24
	- <b>24</b> 7.83	- <b>22</b> 7.61	-20			-14 6.99	- <b>12</b> 6.89	- <b>10</b> 6.80	-8 6.73	-6	-4 6.65	- <b>2</b> 6.63	0 6.62	2 6.64	f Ol	6.71	vat 8 6.77	0 <b>ry</b> 10 6.84	12 6.94	2h a 14 7.05	16 7.18	18 7.33	20 7.51	22 7.70	24 7.92
5.5	- <b>24</b> 7.83 7.81	-22 7.61 7.59	- <b>20</b> 7.42 7.41	-18 7.26 7.24	-16 7.11 7.10	-14 6.99 6.98	-12 6.89 6.87	-10 6.80 6.79	- <b>8</b> 6.73 6.72	- <b>6</b> 6.68 6.67	6.65 6.64	- <b>2</b> 6.63 6.62	0 6.62 6.62	2 6.64 6.63	4 6.66 6.66	6	8	10 6.84 6.84	12 6.94 6.94	14 7.05 7.05	16 7.18 7.18	18 7.33 7.34	20 7.51 7.51	22 7.70 7.71	24 7.92 7.93
5.5 5	-24 7.83 7.81 7.79	-22 7.61 7.59 7.57	-20	-18	-16	-14 6.99	- <b>12</b> 6.89	- <b>10</b> 6.80	-8	-6	-4 6.65	- <b>2</b> 6.63	0	6.64 6.63 6.62	4	6	8	10	12 6.94	14	16 7.18	18 7.33	20 7.51	22 7.70 7.71 7.71	24 7.92 7.93 7.94
5.5 5 4.5	- <b>24</b> 7.83 7.81	-22 7.61 7.59	-20 7.42 7.41 7.39	-18 7.26 7.24 7.22	-16 7.11 7.10 7.08	-14 6.99 6.98 6.96	-12 6.89 6.87 6.86	-10 6.80 6.79 6.78	-8 6.73 6.72 6.71	-6 6.68 6.67 6.66	-4 6.65 6.64 6.63	-2 6.63 6.62 6.61	0 6.62 6.62 6.61	2 6.64 6.63	4 6.66 6.65	6.71 6.70 6.70	8 6.77 6.76 6.76	10 6.84 6.84 6.84	12 6.94 6.94 6.94	14 7.05 7.05 7.05	16 7.18 7.18 7.19	18 7.33 7.34 7.34	20 7.51 7.51 7.52	22 7.70 7.71	24 7.92 7.93
5.5 5 4.5 4 3.5	-24 7.83 7.81 7.79 7.76 7.75 7.73	-22 7.61 7.59 7.57 7.56 7.54 7.52	-20 7.42 7.41 7.39 7.37	-18 7.26 7.24 7.22	-16 7.11 7.10 7.08 7.07	-14 6.99 6.98 6.96 6.95	-12 6.89 6.87 6.86 6.85	-10 6.80 6.79 6.78 6.77	-8 6.73 6.72 6.71 6.70	-6 6.68 6.67 6.66 6.65	-4 6.65 6.64 6.63 6.62	-2 6.63 6.62 6.61 6.61	0 6.62 6.62 6.61 6.61	6.64 6.63 6.62 6.62	4 6.66 6.65 6.65	6.71 6.70 6.70	8 6.77 6.76 6.76	10 6.84 6.84 6.84	12 6.94 6.94 6.94 6.94	14 7.05 7.05 7.05	16 7.18 7.18 7.19 7.19	18 7.33 7.34 7.34 7.34	20 7.51 7.51 7.52 7.52	22 7.70 7.71 7.71 7.72	24 7.92 7.93 7.94 7.95
5.5 5 4.5 4 3.5 3	-24 7.83 7.81 7.79 7.76 7.75 7.73 7.71	-22 7.61 7.59 7.57 7.56 7.54 7.52 7.51	-20 7.42 7.41 7.39 7.37 7.35 7.34 7.33	-18 7.26 7.24 7.22 7.21 7.19 7.18 7.17	-16 7.11 7.10 7.08 7.07 7.06 7.04 7.03	-14 6.99 6.98 6.96 6.95 6.94 6.93 6.92	-12 6.89 6.87 6.86 6.85 6.84 6.83 6.83 6.82	-10 6.80 6.79 6.78 6.77 6.76 6.75 6.74	8 6.73 6.72 6.71 6.70 6.69 6.69 6.68	-6 6.68 6.67 6.66 6.65 6.65 6.64 6.64	-4 6.65 6.64 6.63 6.62 6.62 6.61 6.61	-2 6.63 6.62 6.61 6.61 6.60 6.60 6.59	0 6.62 6.61 6.61 6.60 6.60 6.60	2 6.64 6.63 6.62 6.62 6.62 6.61 6.61	4 6.66 6.65 6.65 6.65 6.65 6.65	6.71 6.70 6.70	8 6.77 6.76 6.76	10 6.84 6.84 6.84 6.84 6.84 6.84 6.85	12 6.94 6.94 6.94 6.94 6.94 6.94 6.95	14 7.05 7.05 7.05 7.05 7.06 7.06 7.07	16 7.18 7.18 7.19 7.19 7.19 7.20 7.20	18 7.33 7.34 7.34 7.34 7.35 7.36 7.36	20 7.51 7.51 7.52 7.52 7.53 7.54 7.55	22 7.70 7.71 7.71 7.72 7.73 7.74 7.75	24 7.92 7.93 7.94 7.95 7.96 7.97 7.98
5.5 5 4.5 4 3.5 3 2.5	-24 7.83 7.81 7.79 7.76 7.75 7.73 7.71 7.69	-22 7.61 7.59 7.57 7.56 7.54 7.52 7.51 7.49	-20 7.42 7.41 7.39 7.37 7.35 7.35 7.34 7.33 7.31	-18 7.26 7.24 7.22 7.21 7.19 7.18 7.17 7.16	-16 7.11 7.08 7.07 7.06 7.04 7.03 7.02	-14 6.99 6.98 6.95 6.94 6.93 6.92 6.91	-12 6.89 6.87 6.86 6.85 6.84 6.83 6.83 6.82 6.81	-10 6.80 6.79 6.78 6.77 6.76 6.75 6.74 6.74	8 6.73 6.72 6.71 6.70 6.69 6.69 6.68 6.68	6 6.68 6.67 6.65 6.65 6.65 6.64 6.64 6.63	-4 6.65 6.64 6.63 6.62 6.62 6.61 6.61 6.61	-2 6.63 6.62 6.61 6.60 6.60 6.59 6.59	0 6.62 6.61 6.61 6.60 6.60 6.60 6.59	2 6.64 6.63 6.62 6.62 6.61 6.61 6.61	4 6.66 6.65 6.65 6.65 6.65 6.65 6.65	6 6.71 6.70 6.70 6.70 6.70 6.70 6.70	8 6.77 6.76 6.76	10 6.84 6.84 6.84 6.84 6.84 6.85 6.85	12 6.94 6.94 6.94 6.94 6.94 6.95 6.95	14 7.05 7.05 7.05 7.06 7.06 7.06 7.07 7.07	16 7.18 7.19 7.19 7.19 7.20 7.20 7.21	18 7.33 7.34 7.34 7.35 7.36 7.36 7.36 7.37	20 7.51 7.51 7.52 7.52 7.53 7.54 7.55 7.56	22 7.70 7.71 7.71 7.72 7.73 7.74 7.75 7.76	24 7.92 7.93 7.94 7.95 7.96 7.97 7.98 7.99
5.5 5 4.5 4 3.5 3 2.5 2	-24 7.83 7.81 7.79 7.76 7.75 7.73 7.71 7.69 7.68	-22 7.61 7.59 7.57 7.56 7.54 7.52 7.51 7.49 7.48	-20 7.42 7.41 7.39 7.37 7.35 7.34 7.33 7.31 7.30	-18 7.26 7.24 7.22 7.21 7.19 7.18 7.17	-16 7.11 7.00 7.08 7.07 7.06 7.04 7.03 7.02 7.01	-14 6.99 6.98 6.95 6.94 6.93 6.92 6.91 6.90	-12 6.89 6.87 6.86 6.85 6.84 6.83 6.82 6.81 6.81	-10 6.80 6.79 6.78 6.77 6.76 6.75 6.74	8 6.73 6.72 6.71 6.70 6.69 6.69 6.68 6.68 6.68	6 6.68 6.67 6.65 6.65 6.64 6.64 6.63 6.63	-4 6.65 6.64 6.62 6.62 6.61 6.61 6.60 6.60	-2 6.63 6.62 6.61 6.60 6.60 6.59 6.59 6.59	0 6.62 6.61 6.61 6.60 6.60 6.59 6.59	2 6.64 6.63 6.62 6.62 6.62 6.61 6.61 6.61 6.61	4 6.66 6.65 6.65 6.65 6.65 6.65 6.65	6.71 6.70 6.70	8 6.77 6.76 6.76	10 6.84 6.84 6.84 6.84 6.84 6.84 6.85	12 6.94 6.94 6.94 6.94 6.94 6.95 6.95 6.95	14 7.05 7.05 7.05 7.06 7.06 7.07 7.07 7.07	16 7.18 7.19 7.19 7.19 7.20 7.20 7.21 7.22	18 7.33 7.34 7.34 7.34 7.35 7.36 7.36 7.36 7.37 7.38	20 7.51 7.51 7.52 7.52 7.53 7.54 7.55 7.56 7.57	22 7.70 7.71 7.71 7.72 7.73 7.74 7.75 7.76 7.78	24 7.92 7.93 7.94 7.95 7.96 7.97 7.98 7.99 8.01
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#### **Observatory Pitch Angle (deg)**

**Fig. 16** SALTUS momentum unload interval in hours as a function of observatory pitch and roll at (a) BOL and (b) EOL over the SALTUS FOR. Each number in a colored cell corresponds to the unload interval in units of hours. The smaller the number is, the shorter the unload interval is, which indicates greater momentum accumulation in the RWAs at that attitude. Intervals increase with the mission lifetime as propellant is used, and CG migrates closer to CP. The purple boxes in (a) and (b) highlight the SALTUS FOR defined by  $\pm 20$  deg of pitch and  $\pm 5$  deg of roll and show a BOL minimum unload interval of 4.71 h and an EOL minimum unload interval of 6.59 h.

tank arrangement, we simulated many likely SALTUS missions via Monte Carlo simulation, varying the fuel needed for achieving orbit under launch dispersions. We ran this Monte Carlo for approximately a few hundred cases of nominal properties and compared it with the 95th percentile storage capability to demonstrate the adequate propellant capability of the proposed SALTUS design. Furthermore, we note that, for the MU interval calculations, we used a brute force approach for each case, in which we assume that the RWAs are loaded to capacity in one direction and are required to unload fully before loading in the other direction. We have therefore not considered a low torque accumulation plan, which would reduce propellant even further. This calculation is thus very conservative.

The conservative approach to estimating the fuel needed for the SALTUS mission gives us confidence that further design analysis, even if it reveals additional propellant needs, will validate that there is enough propellant storage in our design. It is likely that, with time for more simulation and analysis, we can optimize our propellant storage design further.

## 5.2 Inflation Control System

## 5.2.1 M1 inflation

The ICS is a closed-loop control system that regulates the flow of helium inflatant from four high-pressure (> 4000 psi) storage tanks on the spacecraft's primary structure through gas lines on the boom to M1 and maintains the pressure within M1 to meet the performance requirements over all attitudes and through the mission during science operations. The ICS maintains M1 pressure during science observations at 5.1 Pa  $\pm$  5.1 mPa. The ICS consists of a large number of high TRL components from previous Northrop Grumman missions requiring pressure-regulated systems, where all ICS components have been identified by a commercial catalog number. The pressure in M1 is sensed through six strain gauges made from piezo-electric film bonded to M1 and connected in a four-wire arrangement, located outside the optical clear aperture—see the SALTUS block diagram in Fig. 4. The strain gauge produces a voltage proportional to film strain, which is proportional to pressure and forms the basis of the error signal for the control loop. With large gauge functions, it provides sufficient resolution and accuracy for control of M1's pressure. The baseline approach is to operate this loop as a bang-bang controller, but other control algorithms will be studied in phase A. Also in phase A, the sensor will be exposed to radiation and low temperature to demonstrate that the behavior of the sensor over these environments is suitable for the SALTUS mission.

The control function is housed in the PIE and communicates directly to the "ICS Controller" in the block diagram (Fig. 4). Based on the error signal, helium gas will either flow into M1 or be released from it. The ICS has sufficient resolution that the errors between the continuous loss rate of M1 and the discrete inflow rates have a mean error of a few nmol/sec, allowing the ICS control loop to maintain pressure within requirements. The SALTUS inflatant gas lasts for the required 5 years of mission life under very conservative assumptions (with an allocation of 200 kg; see Table 3) and is likely to last significantly longer under nominal conditions. Factors contributing to inflatant consumption are penetration by MM, creep-induced hole growth, valve and fitting leakage, and cold-to-hot losses,<sup>10</sup> and permeation.<sup>14</sup> The brass board ICS will be part of phase B testing to show that the combined M1 ICS functions together as a system.

## 5.2.2 Micrometeoroids (MM)

MM bombardment causes a linearly increasing leak rate with time, resulting in a time-squared dependence on the inflatant mass.<sup>14,15</sup> To make an accurate estimate of the area of penetrations over time, Northrop Grumman carried out a series of hypervelocity impact tests on representative membranes and produced a model of fragmentation, to accurately determine the total area damaged.<sup>14</sup> Reference 14 outlines these tests, and Ref. 10 modifies this approach to give a calculation of the total area damaged from the full MM flux for membranes of thickness and properties appropriate for SALTUS. As an additional contingency factor to create a worst-case expectation of MM penetration, Northrop Grumman also uses an internally developed tool, MADRAT, for the more specific calculations of the system penetration including factors such as orientation, system shielding, orbital velocity, and natural anisotropies in the environmental

flux. MADRAT is validated against NASA's BUMPER code<sup>16</sup> and has specifically included a factor for hole growth due to visco-elastic creep as part of worst-case estimates of gas consumption. Polymeric films as will be used on M1 are expected to have negligible creep as the operating temperature is low and far from the glass transition temperature.<sup>17</sup> The losses due to cold to hot are assumed to be incurred every other observation and taken for the full venting of 0.04 to 0.07 mols, depending on temperature. The vendor-specified valve losses for both internal and external leaks are assumed to be entirely external, then doubled as an additional contingency. Assessment of the inflatant lifetime is performed with worst-case and nominal CBE parameters. The 5-year inflatant lifetime is met under worst-case and nominal conditions.

Finally, we note that, compared with JWST, although the SALTUS lifetime is more sensitive to MM impacts, the wavefront performance of M1 is far less sensitive to these effects. Because JWST has a rigid mirror system, the shape of a damaged rigid mirror element is permanently changed by MM impacts. Crucially, any SALTUS M1 shape change is mitigated by ICS inflation rate adjustments, which reestablish the shape and eliminate residual wavefront error. We refer the reader to Ref. 10 for an in-depth discussion of M1 design, properties, performance, MMs, and lifetime.

# 6 Summary

Northrop Grumman has designed an observatory flight system for the SALTUS NASA APEX mission concept that draws heavily from LEOStar-3 and GEOStar-3 spacecraft product lines, both of which have significant flight heritage in a variety of missions, including NASA science missions. The spacecraft architecture accommodates the SALTUS Payload, thereby delivering unprecedented spectral sensitivity and performance to probe important far-infrared science from space. The SALTUS M1 has a 14-m diameter and is radiatively cooled to <45 K by a two-layer sunshield at ~1000 m<sup>2</sup> per layer. The observatory has access to two 20-deg fields around the ecliptic poles and can cover the entire sky in 6 months. The architecture is fundamentally limited by a two-consumable system driven by propellant and inflatant capacities, and the design and CONOP have been optimized to meet the 5-year mission lifetime and beyond. If selected, the mission would launch in 2032.

#### Code and Data Availability

Data sharing is not applicable to this article as no new data were created or analyzed.

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